

# Anticipating Spectrogram Classification Error With Combinatorial Coverage Metrics

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# Academic Mission

- I am a systems theorist and machine learning engineer.
- I develop and apply systems theory to bridge systems engineering and artificial intelligence.



#### My mission is to develop rigorous first-principles for engineering AI-heavy systems.

"In order to improve your game, you must study the endgame before everything else, for whereas the endings can be studied and mastered by themselves, the middle and the opening must be studied in relation to the endgame."

- Jose Raul Capablanca

# **Executive Summary**

Combinatorial coverage metrics have a high correlation with accuracy on batches of spectrograms, therefore they can be used to anticipate error in spectrogram classification.

# Deep Spectrogram Classification

- Variety of applications in literature including to coexist with and discern primary user, spectrum sharing scenarios, spectrum occupancy reconstruction
- Also there exists advanced deep architectures for supervised problem



F. Paisana, A. Selim, M. Kist, P. Alvarez, J. Tallon, C. Bluemm, A. Puschmann, and L. DaSilva, "Context-aware cognitive radio using deep learning," in 2017 IEEE International Symposium on Dynamic Spectrum Access Networks (DySPAN). IEEE, 2017, pp. 1–2.

# Preliminaries on Coverage

**Definition 1.** *t*-way Combinatorial Coverage. Consider a universe with *k* factors such that  $\mathcal{U}$  is the set of all valid *k*-way value combinations. Let  $\mathcal{U}^t$  be the set of valid *t*-way combinations. Given a set of data  $D \subseteq \mathcal{U}$ , let  $D^t$  define the set of *t*-way value combinations appearing in *D*. The *t*-way combinatorial coverage of *D* is

$$CC^t(D) = \frac{|D^t|}{|\mathcal{U}^t|},$$

where |D| denotes the cardinality of D.

SDCC is alternatively measures the proportion of valid tway value combinations that appear in one set relative to another set. SDCC is defined in the following [12].

## Preliminaries on Coverage

**Definition 2.** t-way Set Difference Combinatorial Coverage. Let  $D_A$  and  $D_B$  be sets of data, and  $D_A{}^t$  and  $D_B{}^t$  be the corresponding t-way sets of data. The set difference  $D_B{}^t \setminus D_A{}^t$  gives the value combinations that are in  $D_B{}^t$  but that are not in  $D_A{}^t$ . The t-way set difference combinatorial coverage is

$$SDCC^t(D_B, D_A) = \frac{|D_B^t \setminus D_A^t|}{|D_B^t|}.$$

### Method

We propose a method to learn a latent space for spectrograms that is meaningful for coverage analysis of classification accuracy. Our method consists of three steps.

- 1) First, use a deep autoencoder to encode spectrograms from pixel-space to a lower-dimensional representation.
- 2) Second, use metric learning techniques for dimension reduction to further reduce the dimensionality of the encoded spectrograms.
- 3) Last, to discretize the data, apply k-means clustering to the metric learning spaces and to the reconstruction error of the autoencoder.

# Metric Learning Methods

- We use PCA, NCA, and LMNN
  - PCA is principal component analysis
  - NCA is a variation on k-nearest neighbors (KNN) classification that directly maximizes a variant of leave-one-out performance
  - LMNN is a variation on KNN classification that learns a Mahalanobis distance

Cody, Tyler, and Laura Freeman. "Metric Learning Improves the Ability of Combinatorial Coverage Metrics to Anticipate Classification Error." *2023 IEEE International Conference on Software Testing, Verification and Validation Workshops (ICSTW)*. IEEE, 2023.





# Encoding

#### Without filter



#### **Cross-Validation Results**



### Batch Results Plot



## Batch Results Table

#### TABLE I MEAN AND STANDARD DEVIATION OF PEARSON CORRELATIONS BETWEEN ACCURACY AND SDCC

Batch Size	t=2	t=3	t=4
100	(-0.87, 0.16)	(-0.94, 0.03)	(-0.95, 0.04)
200	(-0.84, 0.28)	(-0.80, 0.58)	(-0.77, 0.58)
300	(-0.93, 0.02)	(-0.95, 0.03)	(-0.93, 0.08)
400	(-0.92, 0.07)	(-0.96, 0.04)	(-0.97, 0.02)
500	(-0.90, 0.11)	(-0.94, 0.07)	(-0.95, 0.05)

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