

DEEP LEARNING OF PHASE-FIELD SIMULATED DOMAIN STRUCTURE OF FERROELECTRICS FOR REFLECTARRAY ANTENNAS

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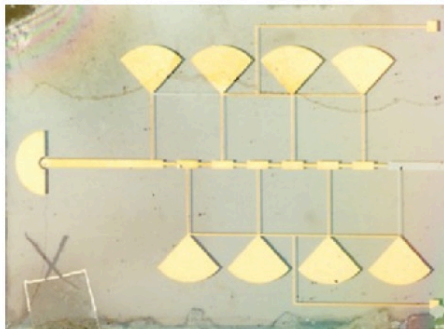
¹University of Idaho

²Michigan State University



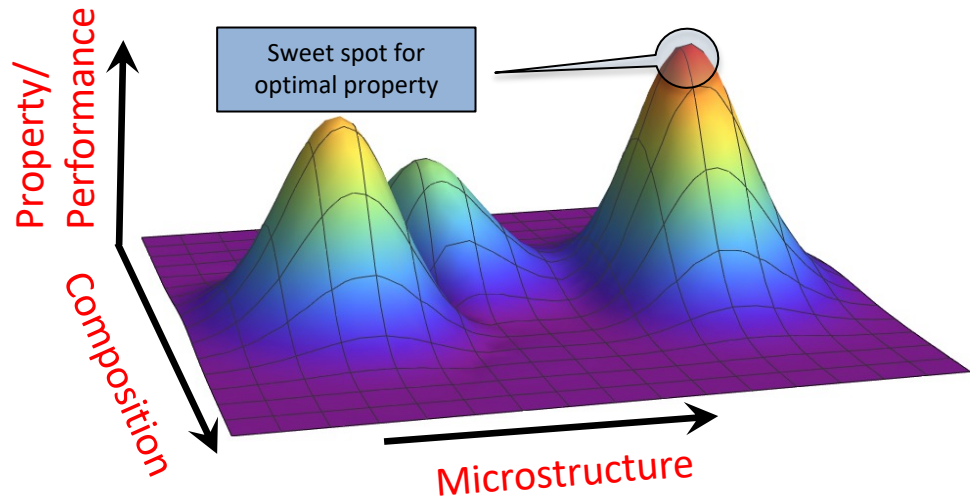
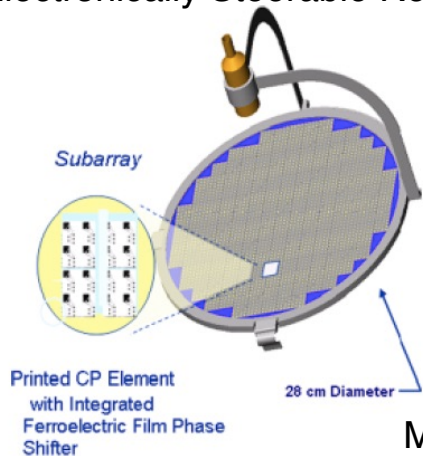
Materials Design for Ferroelectric Reflectarray Antenna

Coupled Microstrip Phase Shifter (CMPS)



10,000

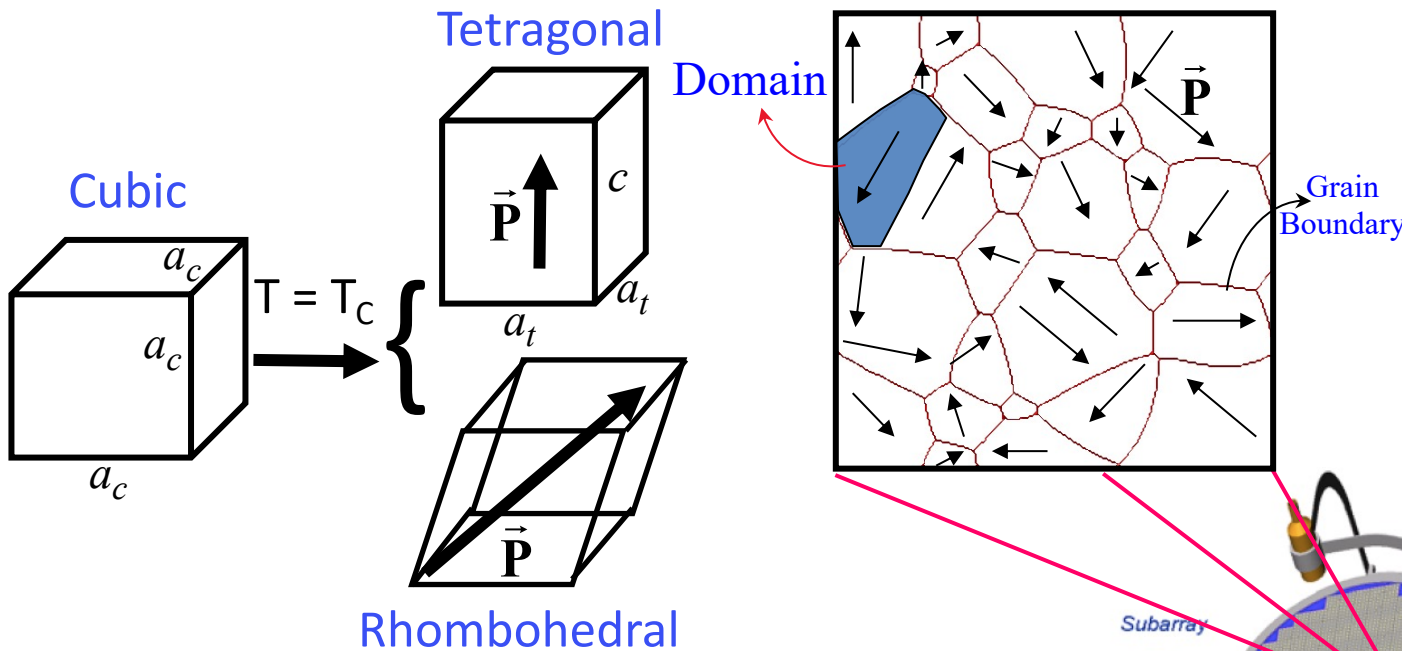
Electronically Steerable Reflectarray Antenna



Potential Ferroelectric Compositions Investigated:

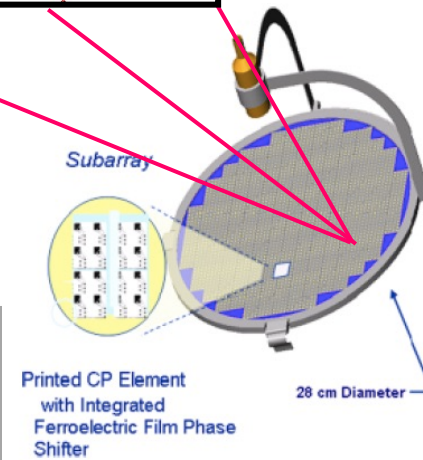
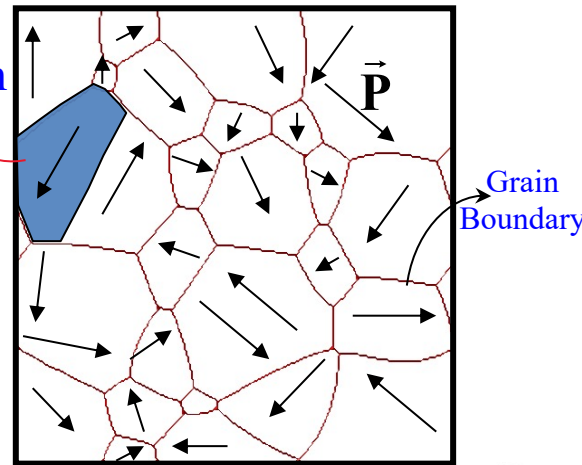
- SrTiO_3
- $\text{Ba}_x\text{Sr}_{1-x}\text{TiO}_3$
- $(\text{Pb},\text{La})(\text{Zr},\text{Ti})\text{O}_3$
- PbSr TiO_3

Microstructure/Domain Structure in Ferroelectrics



Inhomogeneities Affecting Polarization Switching in Ferroelectrics

- **Grain boundaries**
- **Twin domains**
- **Free surfaces**
- **Domain walls**
- **Dislocations**



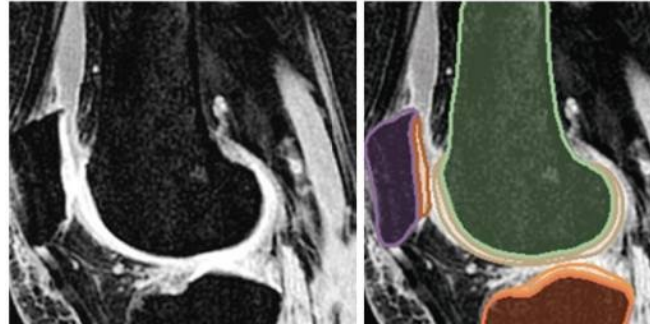
Macroscale device level



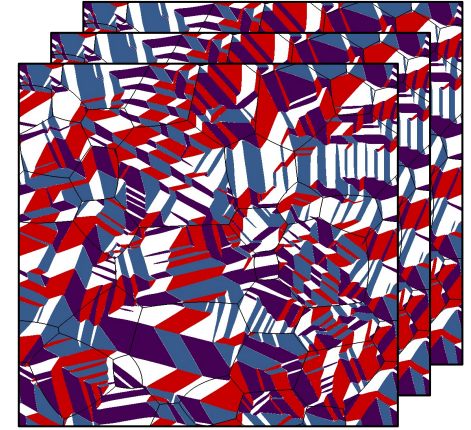
DEEP LEARNING



Self-driving Cars



Smarter Healthcare



Microstructure
Optimization

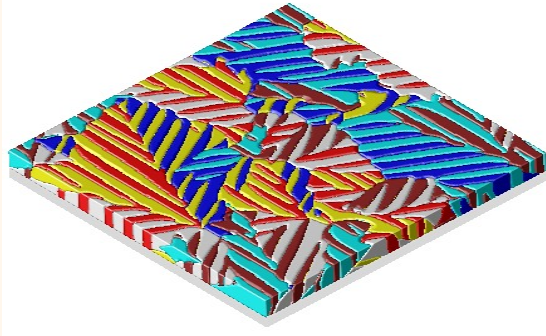
Deep learning can quantitatively analyze patterns in image

Would need tens to hundreds of 1,000s of carefully labeled microstructures

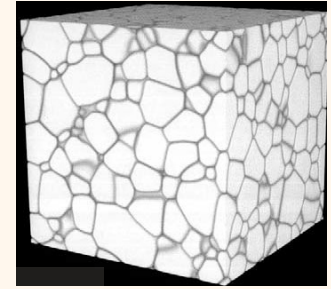
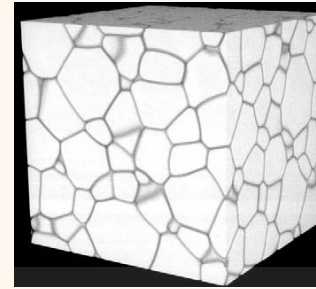
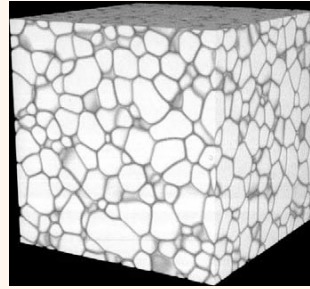
Unlike most experiments, phase-field simulations can generate thousands of microstructures within weeks to months time

Phase-field Simulations of Microstructures

Ferroelectric Domain Structure



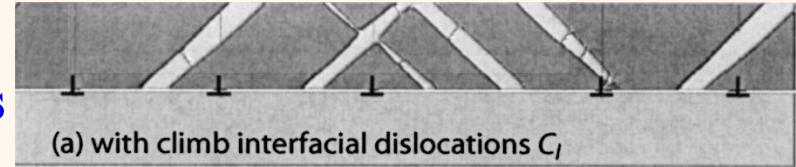
Choudhury and Chen, 2009
Journal cover *J. Am. Ceram. Soc.*



Grain Growth

Krill and Chen, *Acta. Mat.* 2002

Dislocations

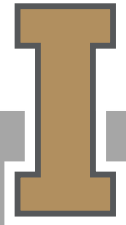


(a) with climb interfacial dislocations C_I

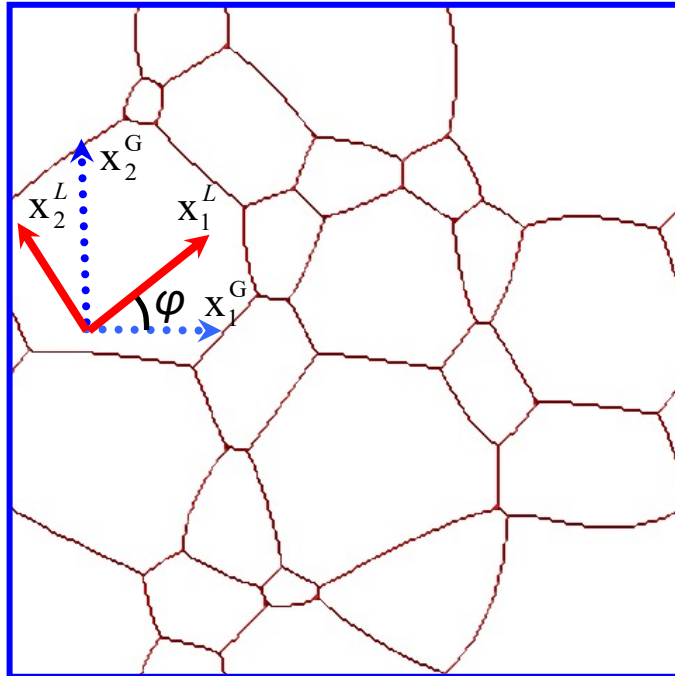
Domain St. in PTO thin films with interfacial dislocations.

Li et. al. *J. Appl. Phys.* 2003

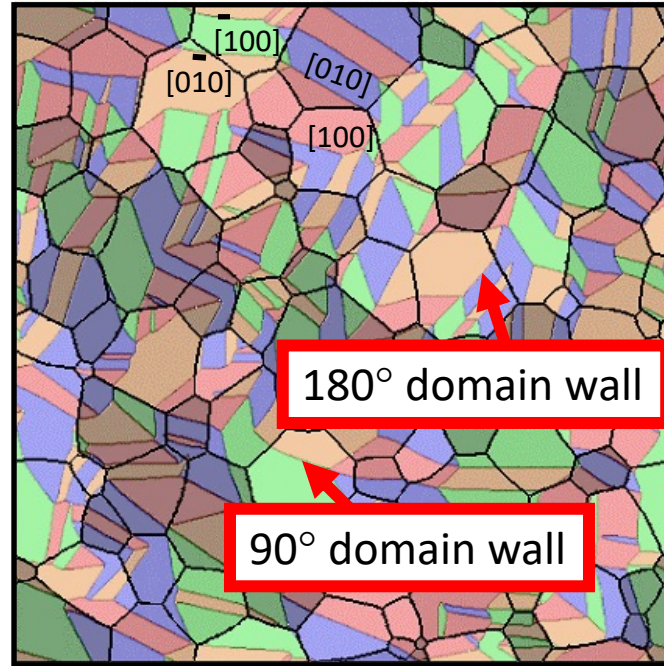
Possible to simulate microstructure
when multiple features coexist



Domain Structure in Polycrystalline PbTiO_3

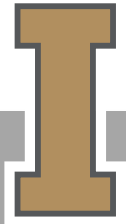


Krill and Chen *Acta Mater.* 50, 3057, 2002

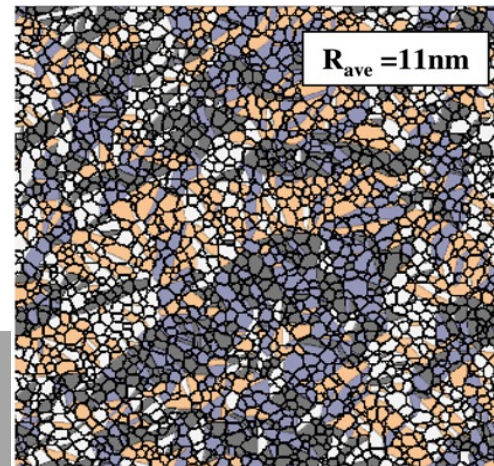
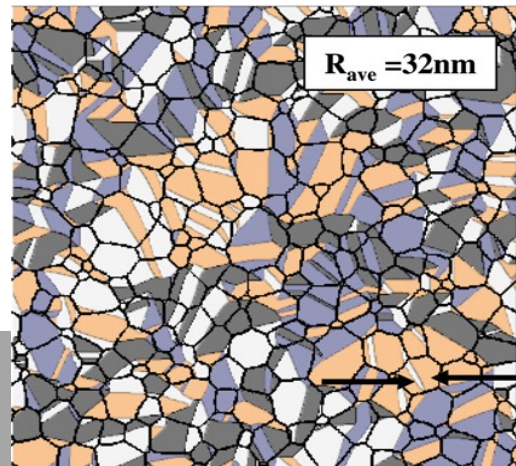
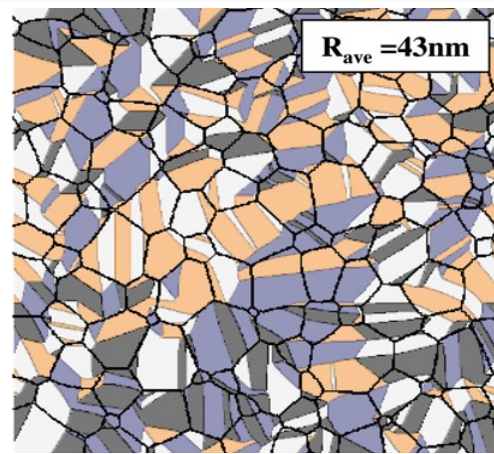
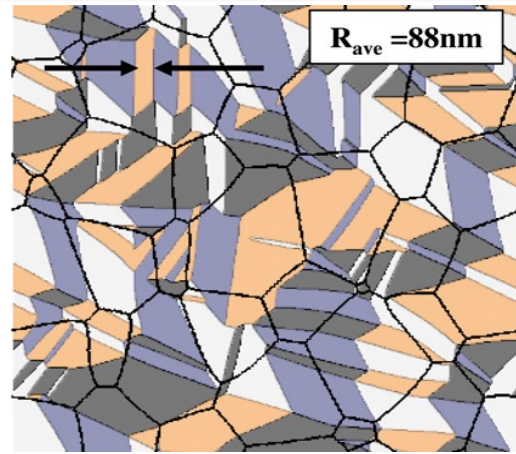


Simulated domain structure of PbTiO_3 ceramics with no applied electric field

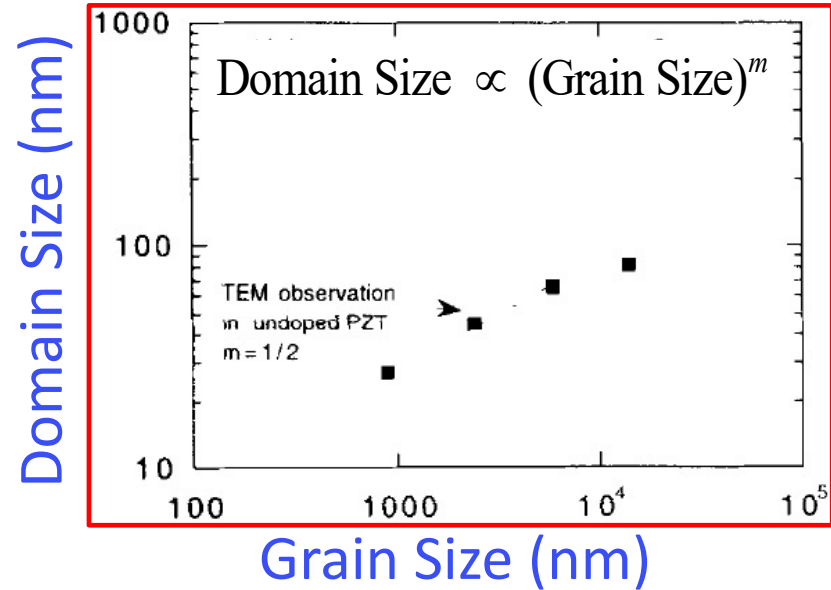
S. Choudhury,
et. al *Acta
Mater.* 2005



Effect of Grain Size on Domain Structure in PbTiO_3



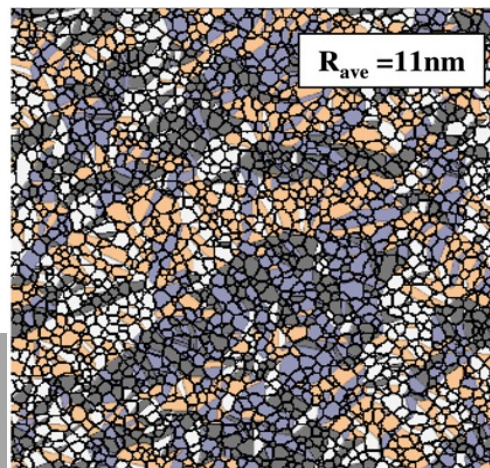
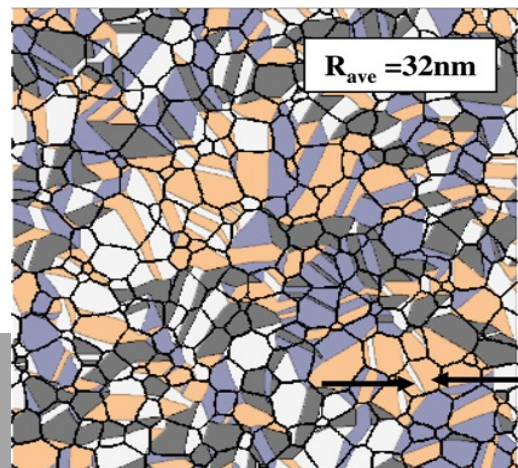
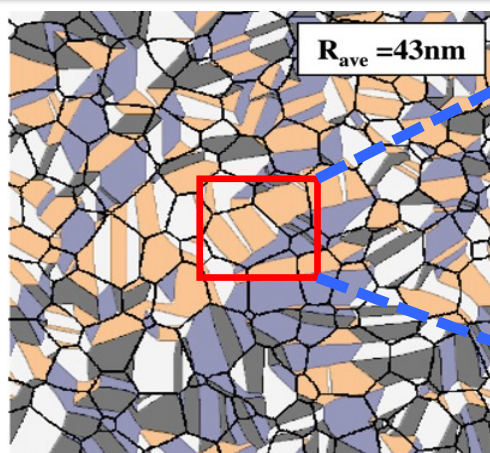
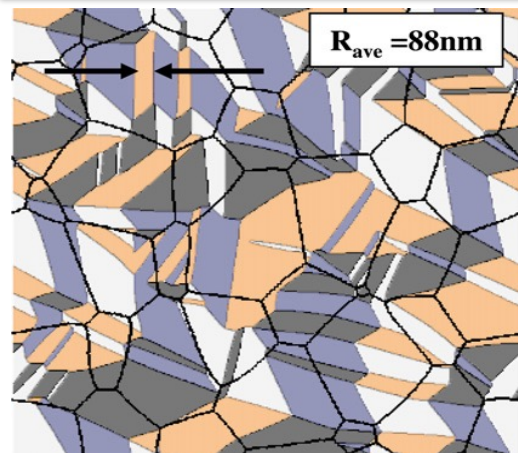
TEM Measured Domain Size



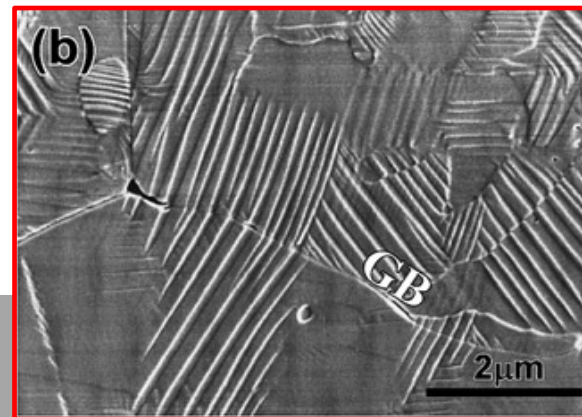
Cao and Randall *J Phys Chem Solids*, 1996

S. Choudhury, et. al *Acta Mater.* 2007

Effect of Grain Size on Domain Structure in PbTiO_3



Domain St. of PZT Ceramics

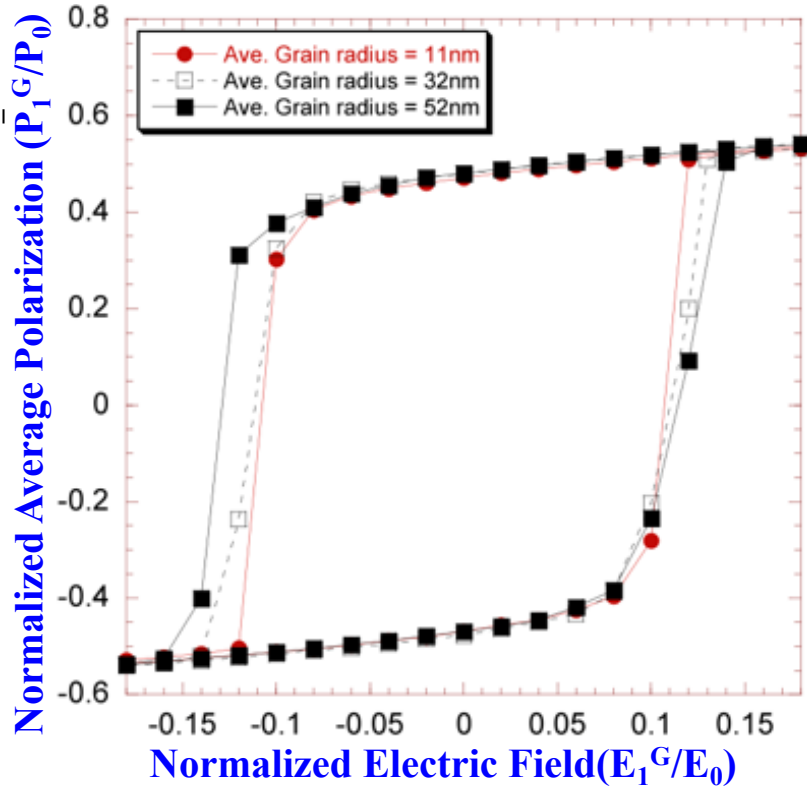


Tsurekawa *et al.*
Scripta Mater., 2007

Ohio

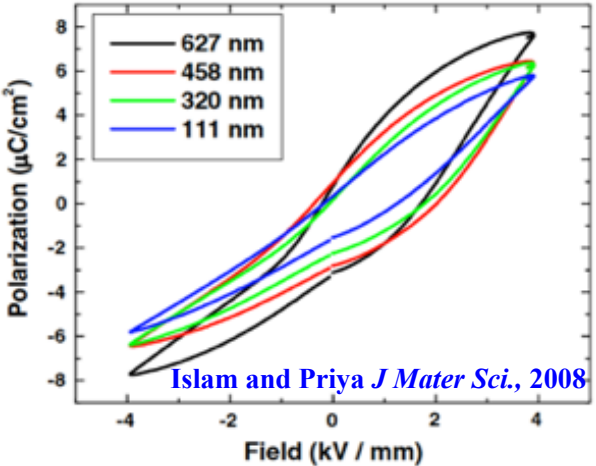
Effect of Grain Size on the Coercive Field in PbTiO_3

Phase-field Simulation

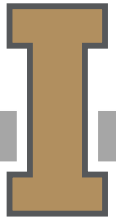


Experimentally Measured

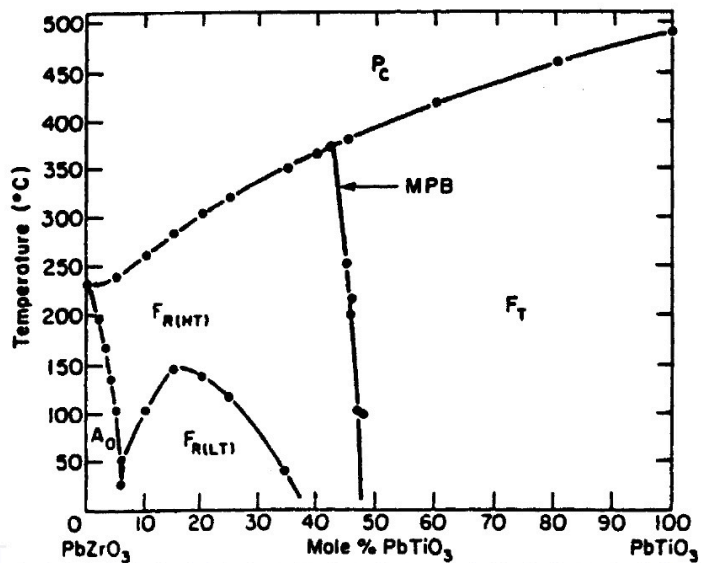
Hysteresis loops of PZT ceramics



	Grain Size	
	627(nm)	111(nm)
Coercive Field	1.7 (kV/mm)	1.2 (kV/mm)

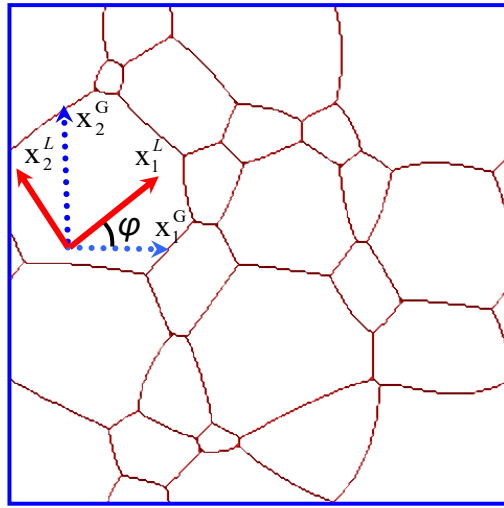


PHASE FIELD SIMULATION OF FERROELECTRIC CERAMICS

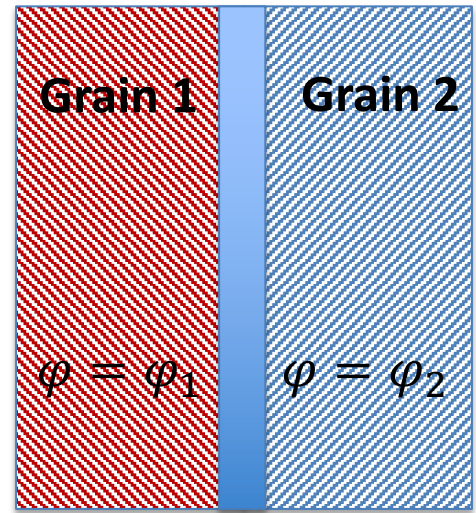


Phase Diagram of PZT

Jaffe et al. 1971



Grain structure and grain orientation



$$T_{bulk} = 479^{\circ}\text{C}$$

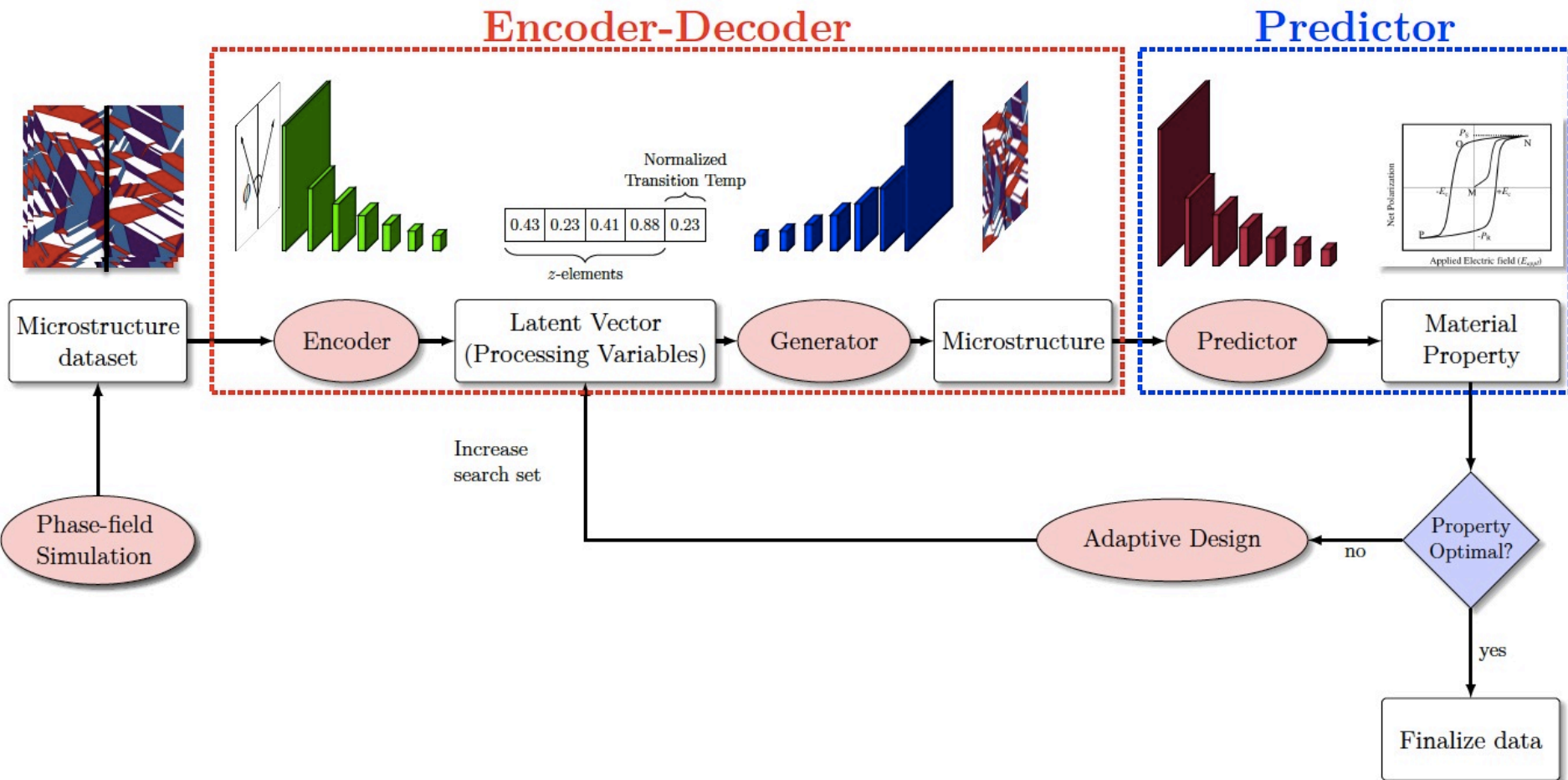
$$T_{gb} = 25 - 479^{\circ}\text{C}$$

Transition Temperature at G.B

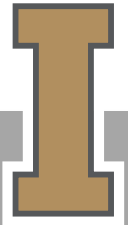
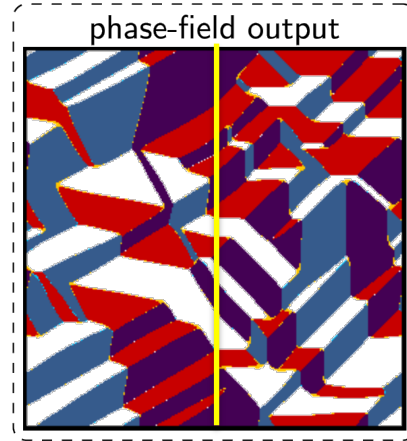
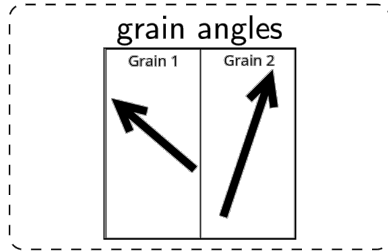
Two processing parameters considered:

- (a) Transition temperature are the grain boundary
- (b) Grain boundary orientation

FLOWCHART OF THE DEEP LEARNING FRAMEWORK

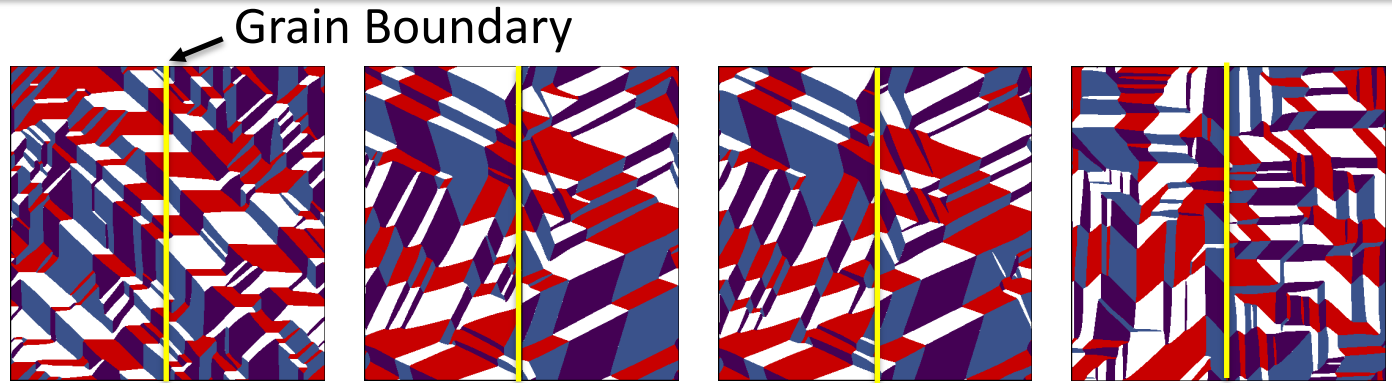


MODEL



Comparison of Microstructures ($T_{GB} = 10^\circ\text{C}$)

Phase-field
Simulated
Microstructures



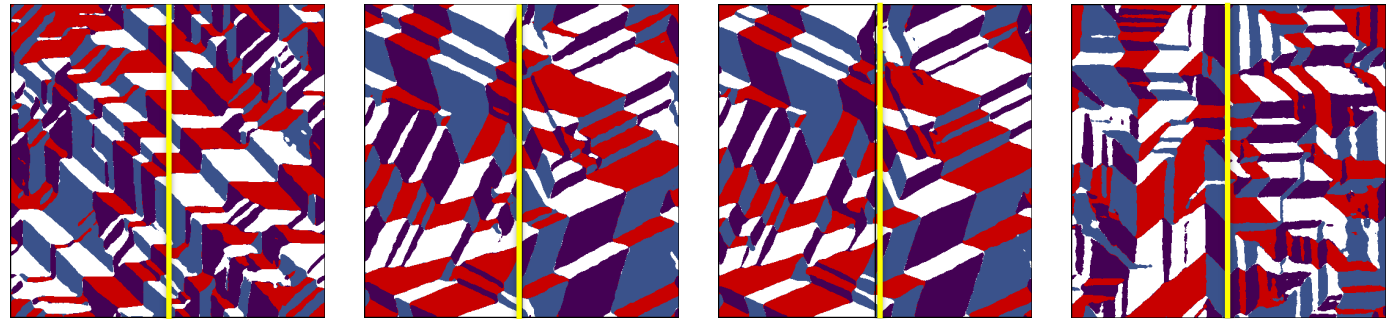
$$\phi = 5^\circ$$

$$\phi = 36^\circ$$

$$\phi = 38^\circ$$

$$\phi = 86^\circ$$

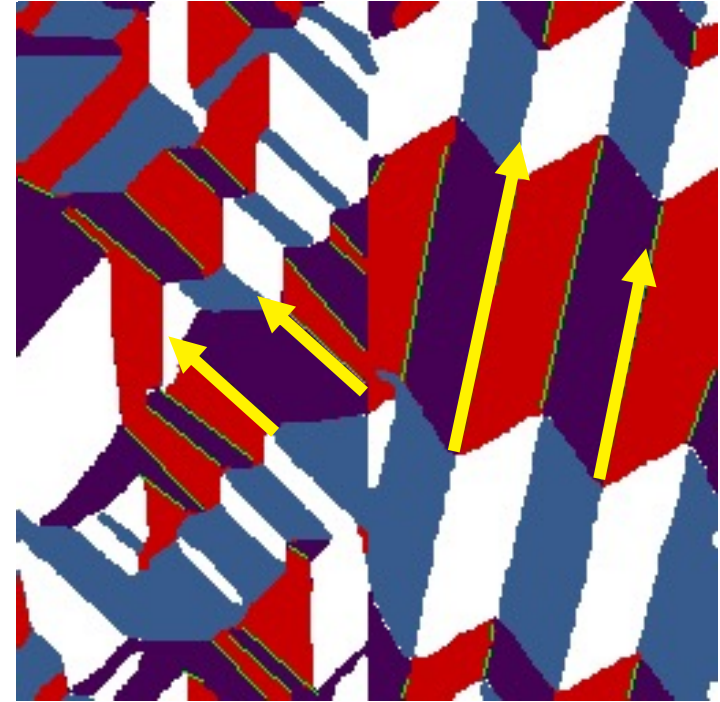
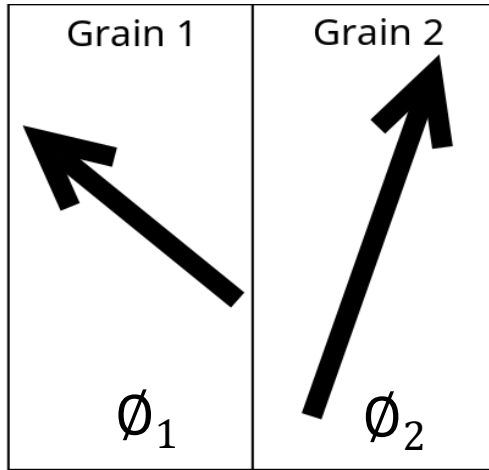
Machine
Predicted
Microstructures



■ $x+$ ■ $x-$ □ $y+$ ■ $y-$

Quantification of Microstructure Prediction

Prediction of Domain Wall Orientation

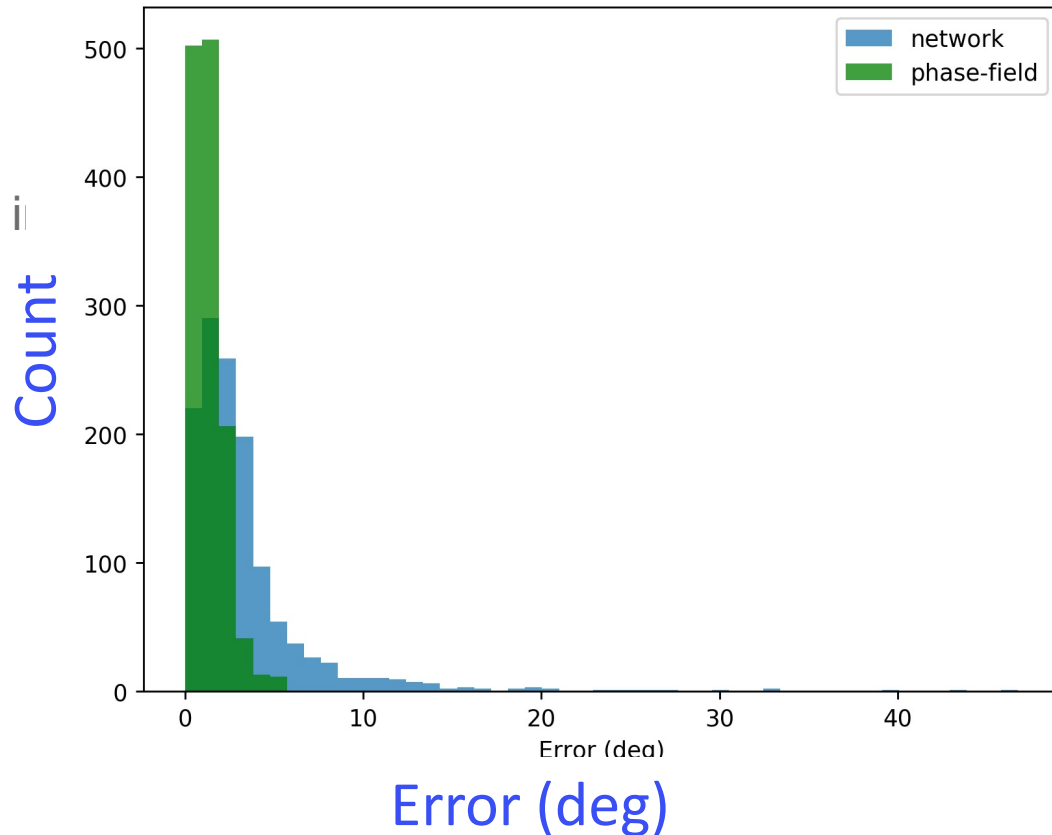


- The orientation of each grain is defined by, ϕ
- For each ϕ domain wall orientation is known
- Our script automatically detects domain wall



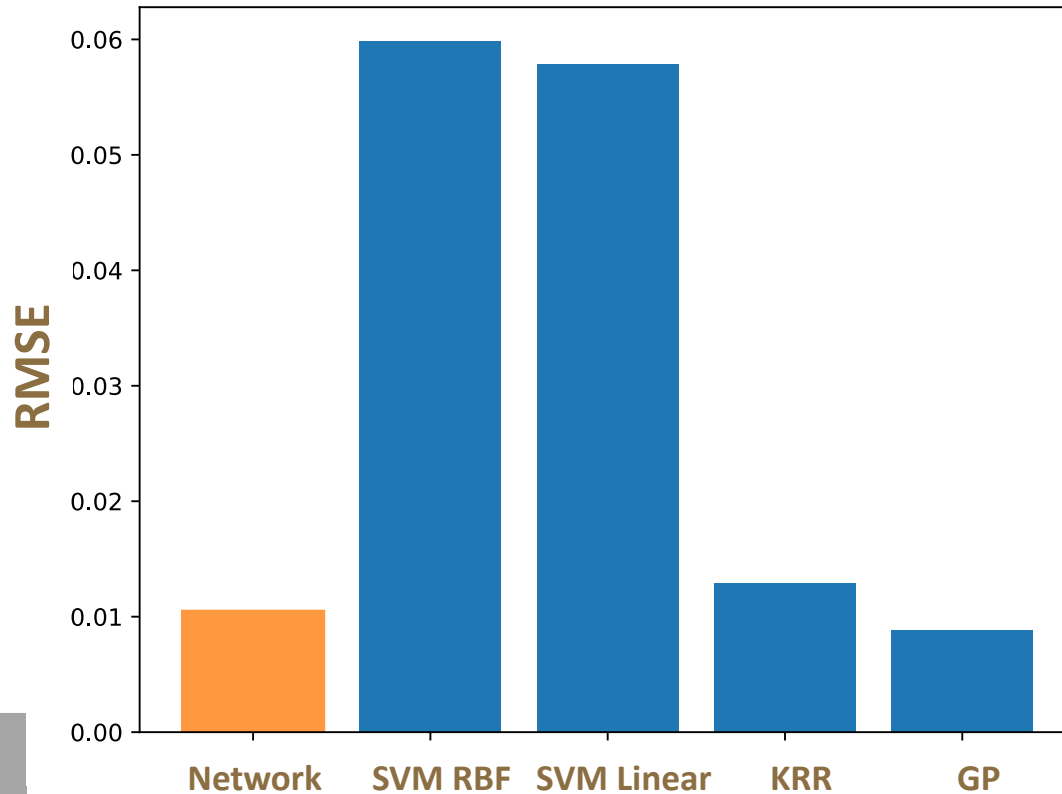
Error in Network Predicted and Phase-field simulated Domain Wall Orientation

- Average angles of same domain wall type within grain
- Average degree deviation from expected domain wall orientation in phase-field simulation: **1.45°**
- Average degree deviation (from expected domain wall orientation for neural net): **2.87°**
- Average prediction within 1.5° error
- **Nearly all cases are within very good estimate of phase-field simulations**



Root Mean Square Error (RMSE) in Predicted Coercive field

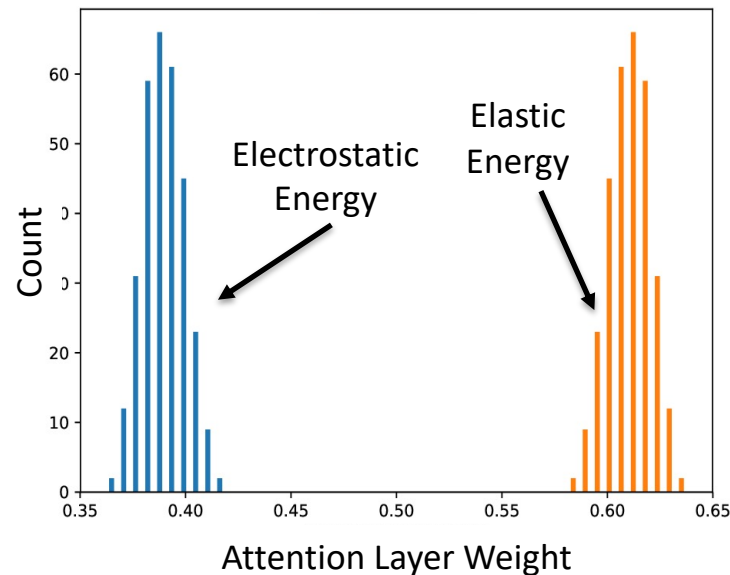
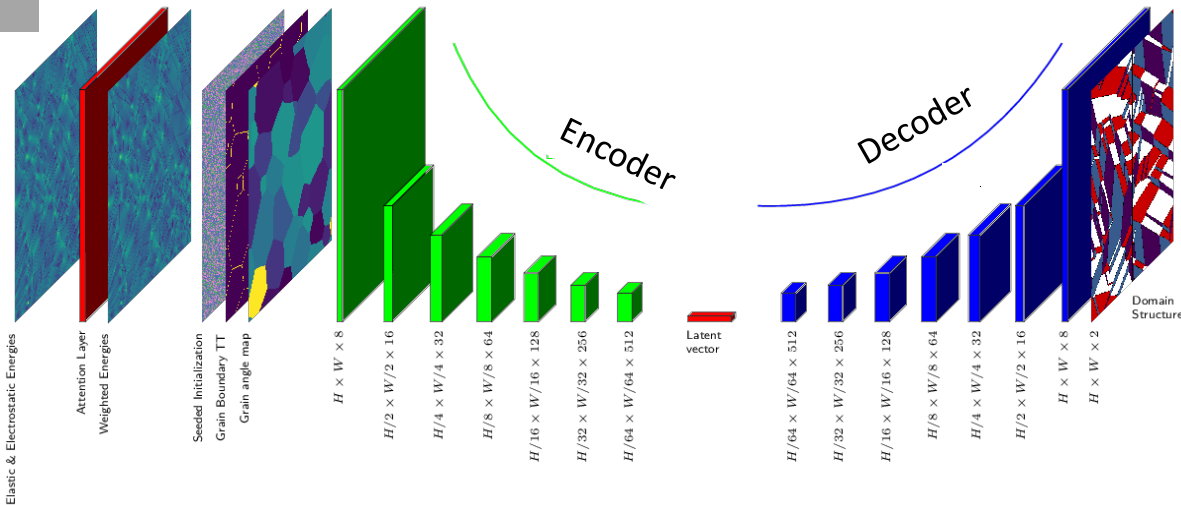
Processing → Microstructure → Property (Coercive Field)



The network prediction of coercive field performs better than those predicted by traditional machine learning on the processing conditions alone.

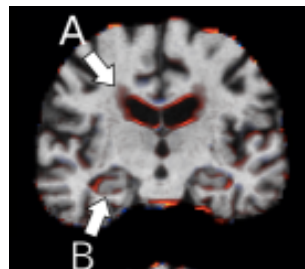
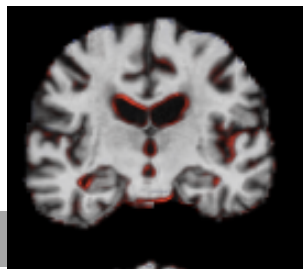


Prediction of Energy Contributions using Attention Layer



Network Predicted Brain Scan

Observed Brain Scan



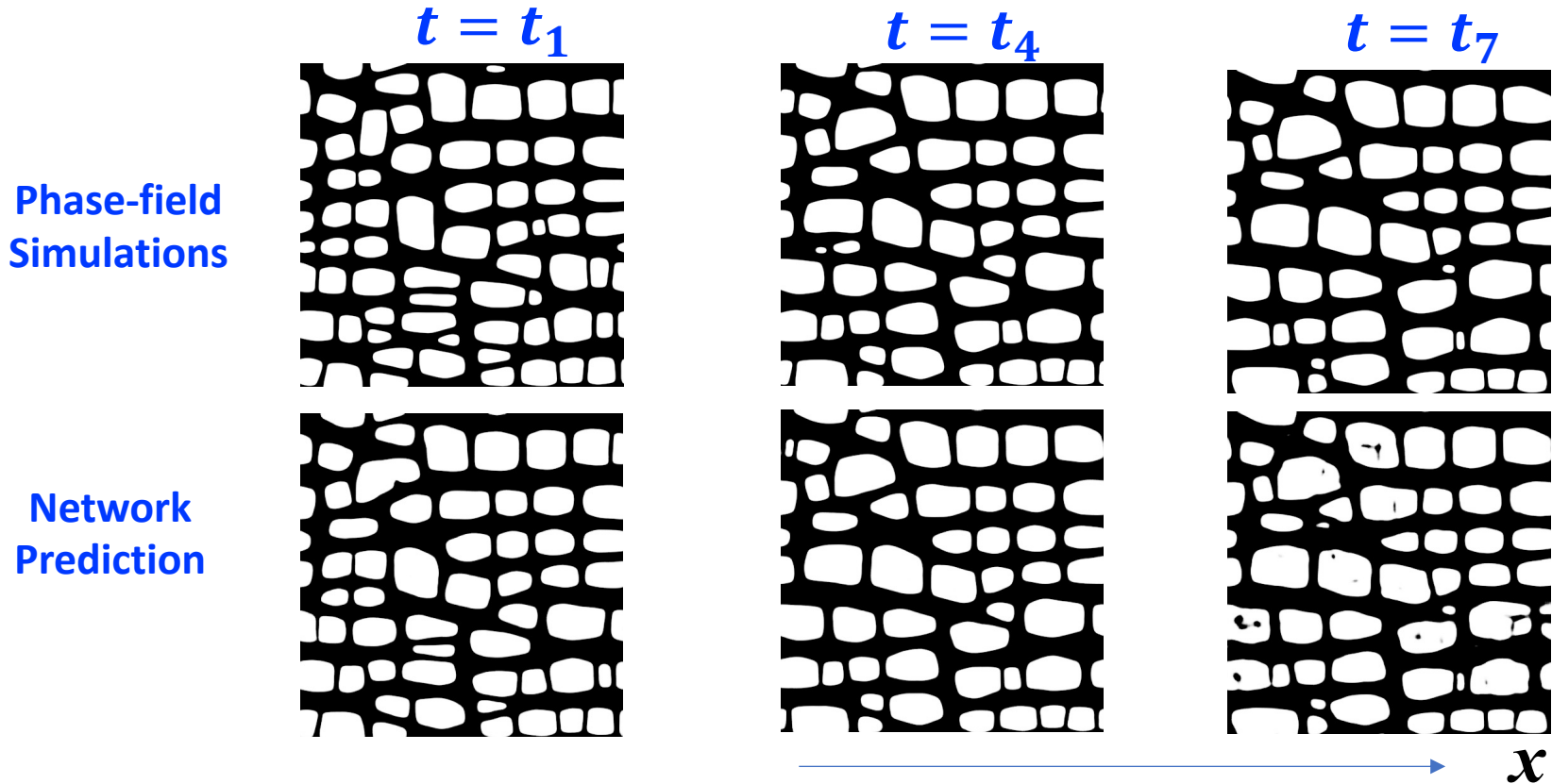
Comparison of regions affected by Alzheimer's disease using attention layer

Added an "attention" layer that weights importance of inputs

Network can provide fundamental insights into microstructure evolution

Baumgartner, C. F. et al. IEEE Conference on Computer Vision and Pattern Recognition (2018).

Comparison of the Microstructure Evolution as 0.2% Strain is Applied in the x Direction to an Initial ($t = t_0$) Microstructure using a Encoder-LSTM-Generator network

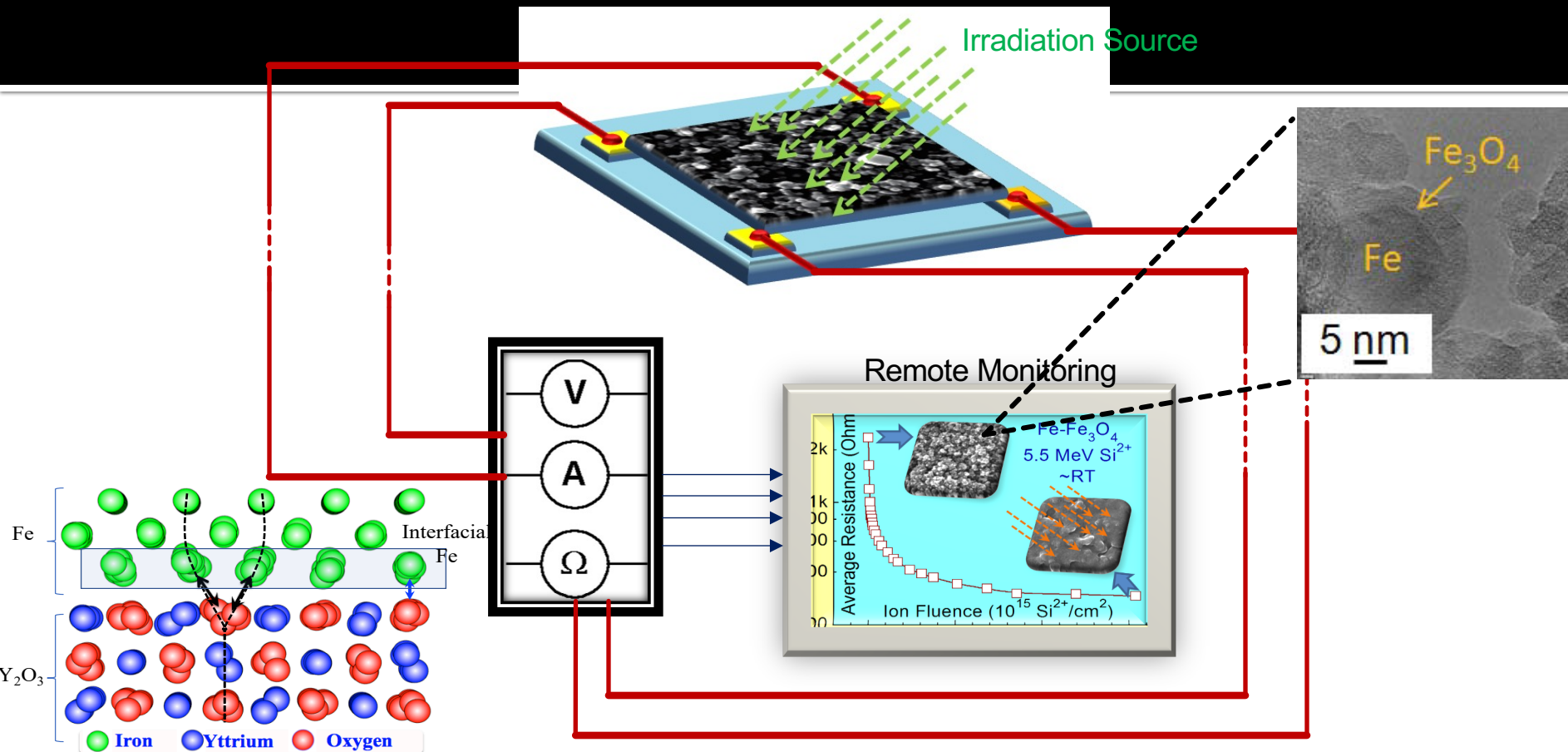


Radiation in Space

Courtesy: Prof. You Qiang (University of Idaho)

- **Galactic Cosmic Rays (GCR)**
 - Protons
 - Particles (Helium)
 - Positrons
 - Neutron
- **Solar Energetic Particles (SEP)**
 - Solar Flares
 - Coronal Mass Ejection (CME) – solar winds

Our In-situ Radiation Monitoring Device



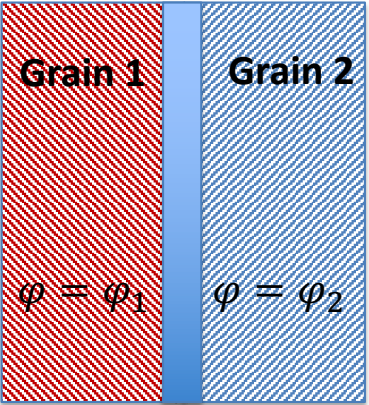
CONCLUDING REMARKS

- Predictive deep learning model is designed for ferroelectric domain structures
- Predicted domains walls match will phase-field model results within 1.5°
- Able to quantify success in learning microstructural properties from phase-field simulations
- Can predict time dependent evolution of microstructures

Acknowledgement: This work was supported financially by a National Science Foundation Graduate Research Fellowship Program under Grant No. 1842399. Part of the calculations were performed at the High Performance Computing Facility at the Idaho National Laboratory, which is supported by the Office of Nuclear Energy of the U.S. Department of Energy under Contract No. DE-AC07-05ID14517.



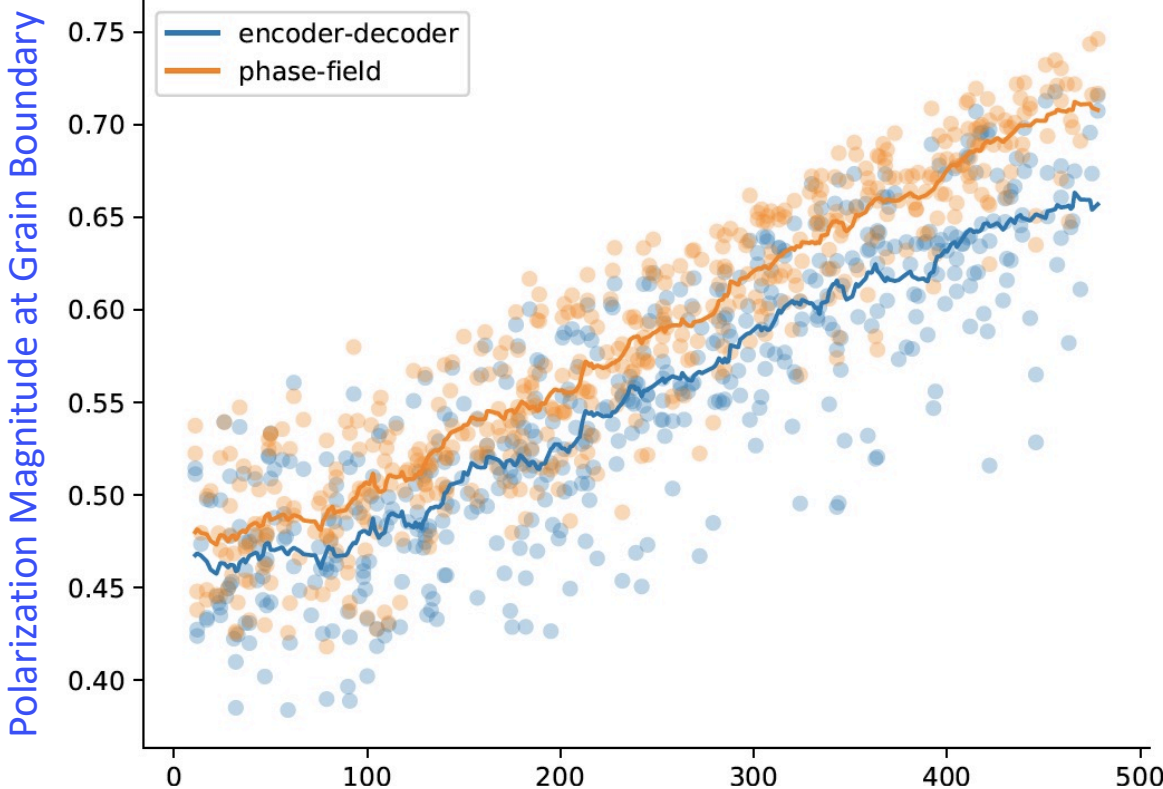
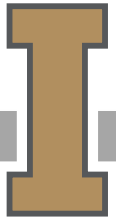
Comparison of Normalized Polarization Magnitude at Grain Boundary



$T_{bulk} = 479^{\circ}C$

$T_{gb} = 25 - 479^{\circ}C$

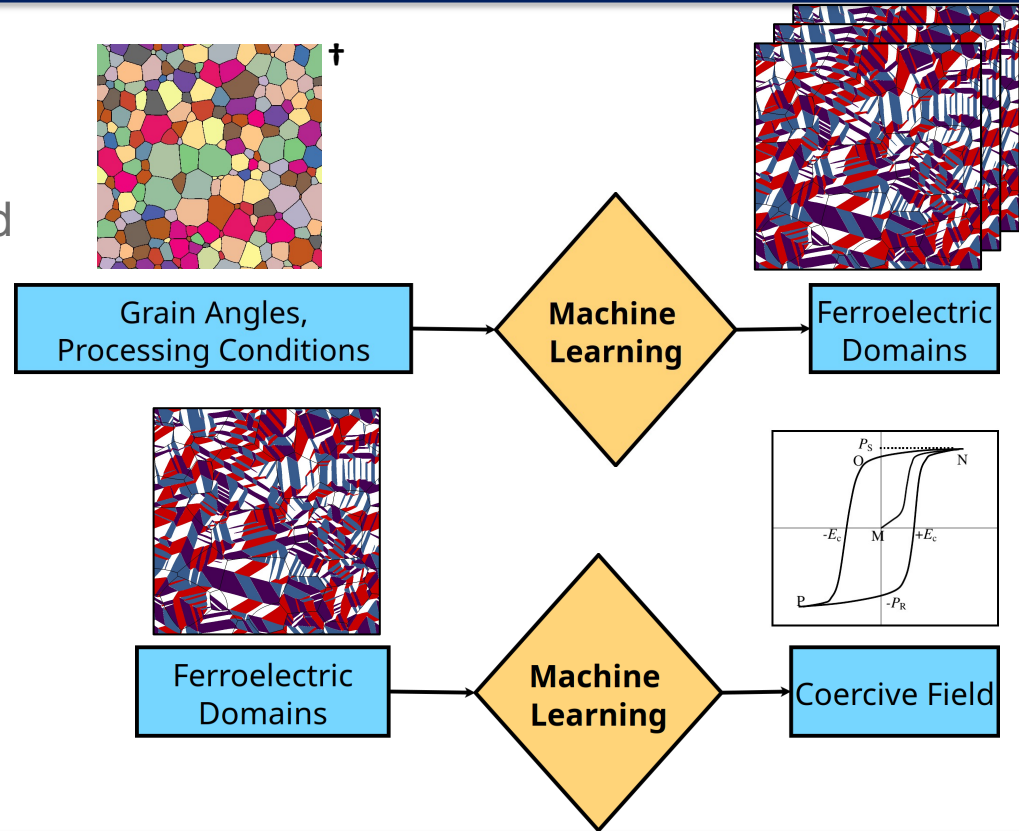
Transition Temperature at G.B



Ferroelectric Transition Temperature at Grain Boundary

METHOD

- 1) Generate samples with phase-field
 - 1,000s of unique samples produced within 2 weeks
- 2) Use processing conditions to predict ferroelectric domain microstructure of PbTiO_3
- 3) Use domains to predict coercive field property

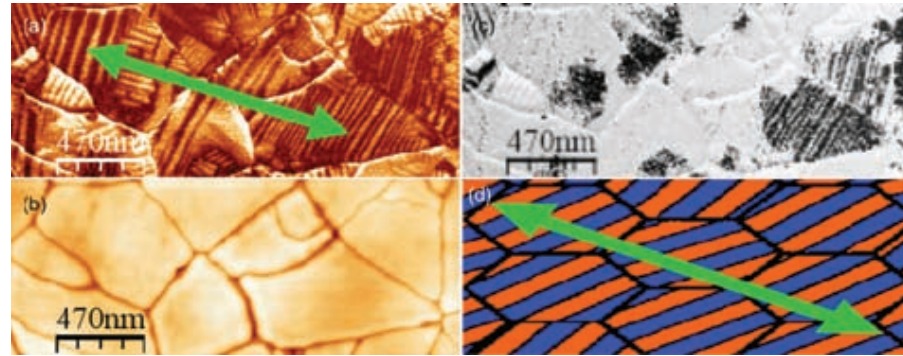


†Grain growth code from C. Krill and L.Q. Chen *Acta. Mat.* **50** 2002

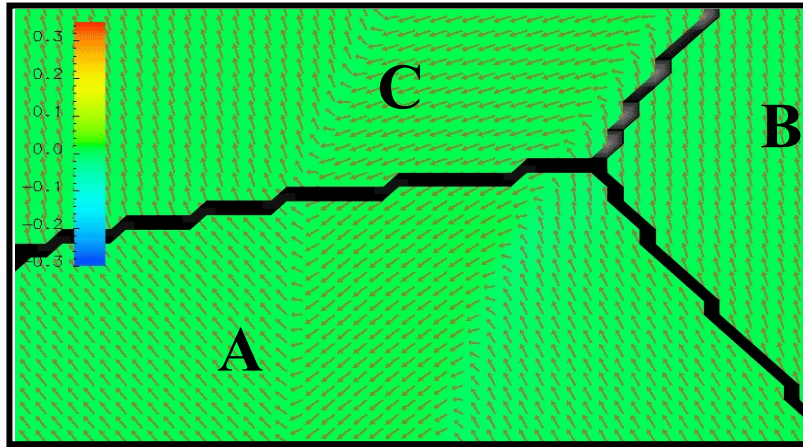


Energetic Contributions toward Domain Formation

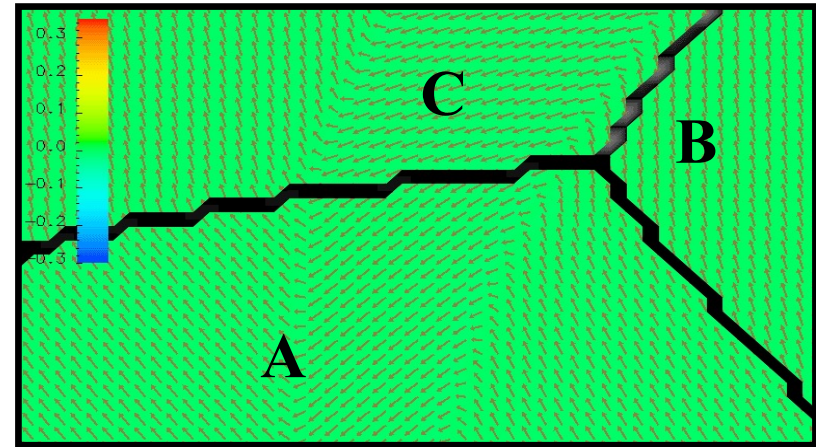
Formation of ferroelectric domain structure is governed by a combination of short-range and long-range interaction



Ivry et. al. *Adv. Func. Mater.* (2014)



Electric energy distribution



Elastic energy distribution

What is the role of individual energies toward of microstructure evolution?

Flowchart of the Encoder-LSTM-Generator network

