

# Machine Learning based Adaptive Predistorter for High Power Amplifier Linearization

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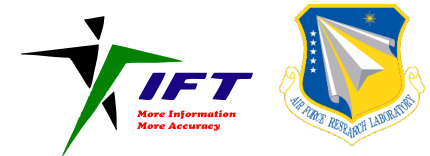


**June 26th, 2019**

# Outline

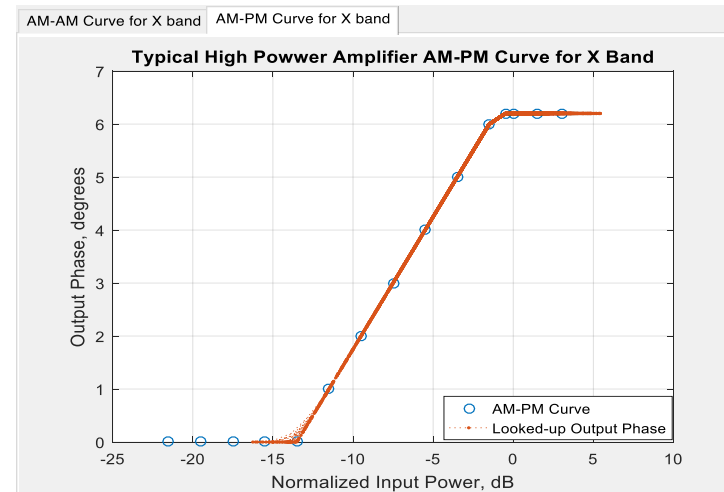
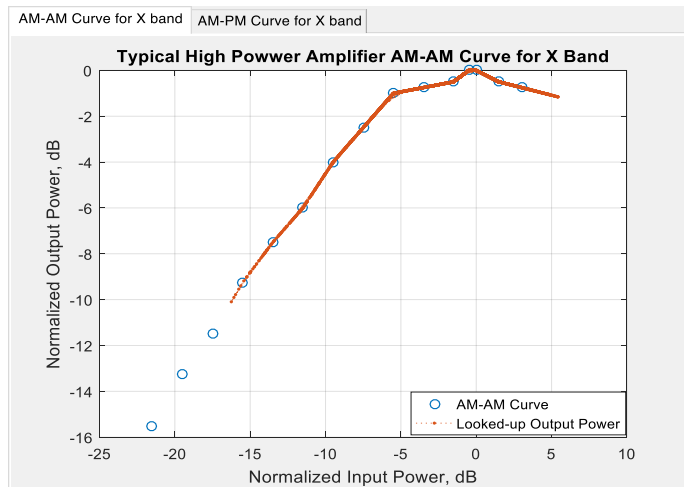
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- **Introduction**
- **CONOPS and System Model**
- **Extended Saleh's Model**
- **Reinforcement Learning based PD Design**
- **Conclusion and Future Work**



# Introduction

- The transponders are equipped with high power amplifiers (HPAs), which, unfortunately, cause nonlinear distortions to the transmitted signal, since HPAs normally operate close to or at saturation, so as to maximize power efficiency.
- This nonlinear distortion can be characterized as amplitude modulation-to-amplitude modulation (AM-AM), and amplitude modulation-to-phase modulation (AM-PM) effects.
- AM-AM and AM-PM distortions cause interference signal non-recognizable.
- The conventional predistortion (PD) method cannot handle the non-linearization problem in the presence of interferences.

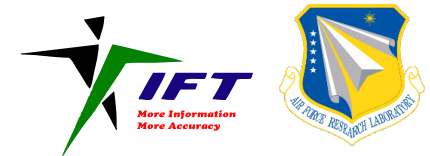


Simulated HPA AM-AM and AM-PM curves for X band Signal

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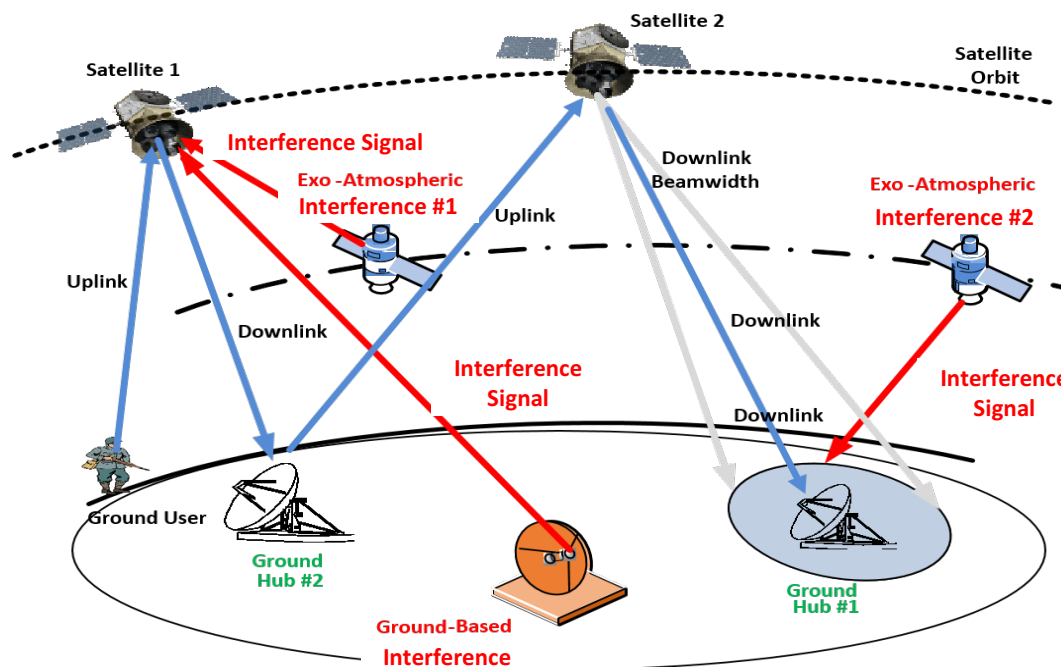
# CONOPS Description

## Satellite 1:

- interference attacks the uplink (U/L) - This is the case of our interest
- Case 1: The interference signal does not cause AM-AM and AM-PM distortion effects
- Case 2: The interference signal power causes the HPA to operate at saturation.

## Satellite 2:

- interference attacks the downlink (D/L) signal
- interference signal on the D/L does not cause AM-AM and AM-PM distortions and hence it is not of our interest

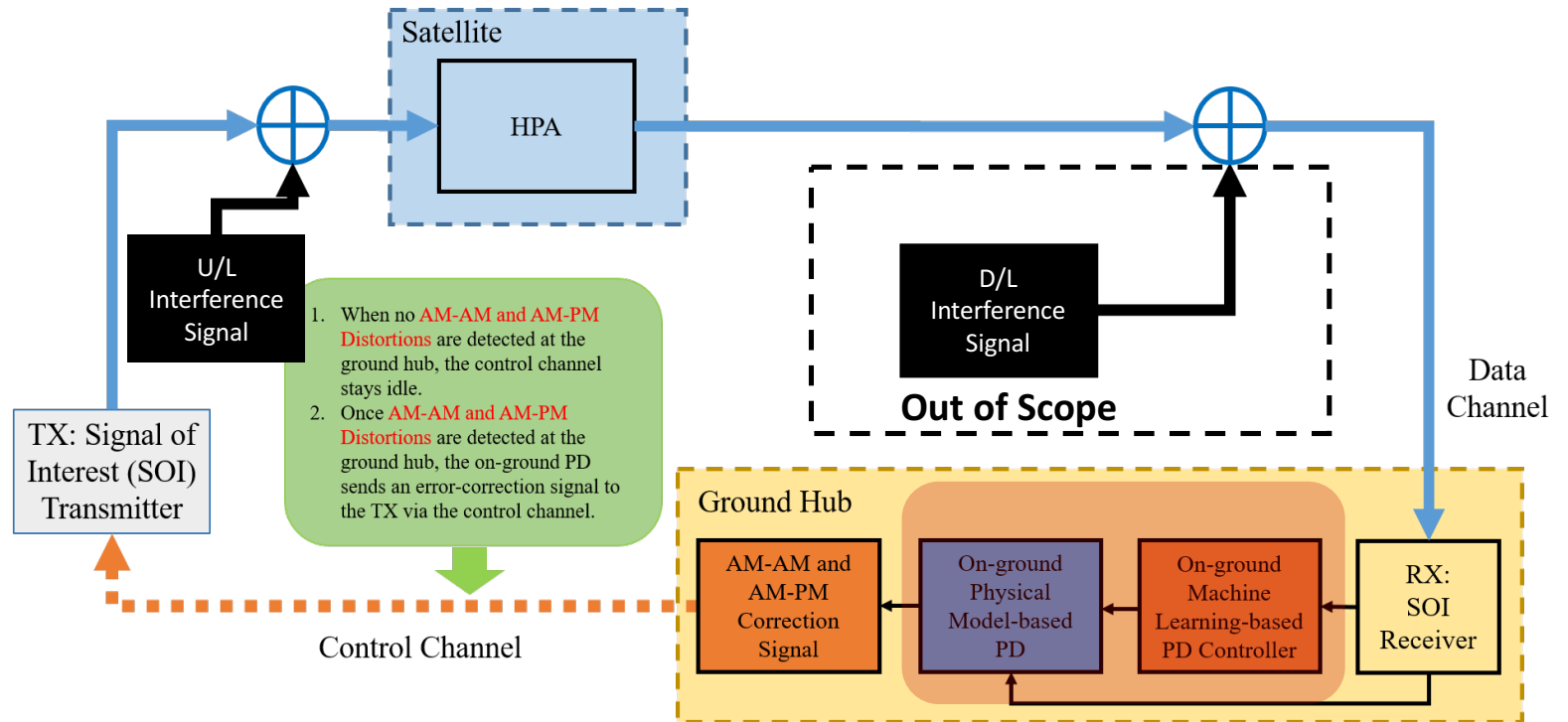


System CONOPS in the presence of interferences

**To linearize satellite transponder in the presence of interferences**

# System Model

- The on-ground PD is able to correct the AM-AM and AM-PM nonlinear distortions by itself when the nonlinearity is not caused by interference signals.
- When interference causes nonlinear distortion to the HPA, the PD controller uses machine learning technique to adjust the parameters of the PD, and send the correction signal to the transmitter.



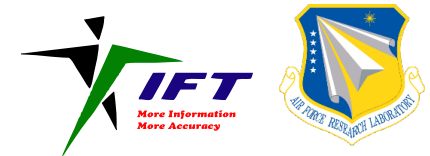
## Proposed on-ground solution for near-term implementation

*This solution only requires us to modify the configurations of the hub and user terminals, which can achieve the goal of low cost.*

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# Extended Saleh's Model: HPA Modeling

Normal Ambient Temperature

Pin(dB)	Pout(dB)	Phase-out(deg.)
P0_in <sub>i</sub> :=	P0_25degC_out <sub>i</sub> :=	Φ_25degC_out <sub>i</sub> :=
-25	-17.25	0.1
-23	-15.5	0.1
-21	-13.5	0.1
-19	-11.5	0.8
-17	-9.5	1.25
-15	-7.5	2.55
-13	-6	6.1
-11	-4	8.55
-9	-2.7	13.1
-7	-1.5	17.71
-5	-0.65	23.82
-3	-0.25	30
-1	0	36.3
0	0.002	40
1	-0.15	43
2	-0.22	45
3	-0.25	47.5
4	-0.75	50
5	-1	53.5
6	-1.2	56

at Room Temperature  
(25 deg C)

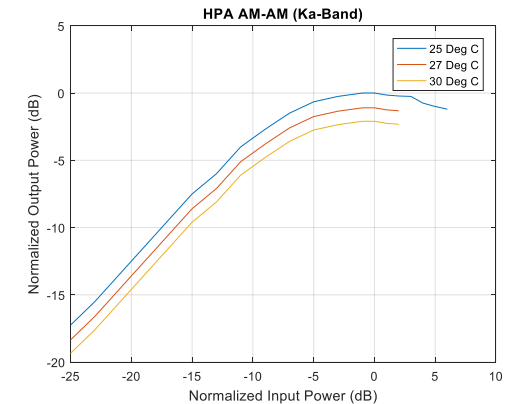
Non-Normal Ambient Temperature

P0_in <sub>i</sub> :=	P0_27degC_out <sub>i</sub> =	Φ_27degC_out <sub>i</sub>
-25	-18.35	-1.7
-23	-16.6	-1.7
-21	-14.6	-1.7
-19	-12.6	-1
-17	-10.6	-0.55
-15	-8.6	0.75
-13	-7.1	4.3
-11	-5.1	6.75
-9	-3.8	11.3
-7	-2.6	15.91
-5	-1.75	22.02
-3	-1.35	28.2
-1	-1.1	34.5
0	-1.098	38.2
1	-1.25	41.2
2	-1.32	43.2

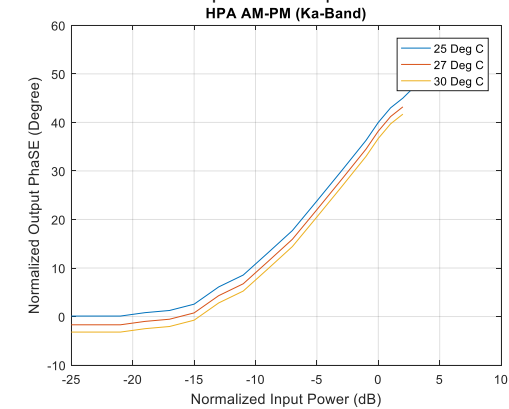
at 27 Deg C

P0_in <sub>i</sub> :=	P0_30degC_out <sub>i</sub> =	Φ_30degC_out <sub>i</sub>
-25	-19.35	-3.2
-23	-17.6	-3.2
-21	-15.6	-3.2
-19	-13.6	-2.5
-17	-11.6	-2.05
-15	-9.6	-0.75
-13	-8.1	2.8
-11	-6.1	5.25
-9	-4.8	9.8
-7	-3.6	14.41
-5	-2.75	20.52
-3	-2.35	26.7
-1	-2.1	33
0	-2.098	36.7
1	-2.25	39.7
2	-2.32	41.7

at 30 Deg C



Measured AM-AM characteristics of Ka-Band HPA with temperature as a parameter

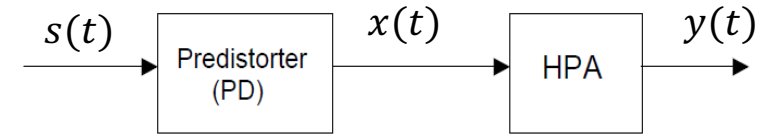


Measured AM-PM characteristics of Ka-Band HPA with temperature as a parameter

T. M. Nguyen, J. Yoh, C. H. Lee, H. T. Tran, and D. M. Johnson, "Modeling of HPA and HPA Linearization Through a Predistorter: Global Broadcasting Service Applications", *IEEE Trans. on Broadcasting*, Vol. 49, No.2, 2003.



# Extended Saleh's Model: HPA Modeling



**Saleh's model** has been proposed for characterizing an HPA's AM-AM and AM-PM distortions accurately. The extended model is designed especially for travelling wave tube (TWT) and /or solid high power amplifiers.

The complex signals  $s(t)$ ,  $x(t)$ , and  $y(t)$  can be written as follows.

$$s(t) = \rho_{s(t)} e^{j\theta_{s(t)}}$$

$$x(t) = \rho_{x(t)} e^{j\theta_{x(t)}}$$

$$y(t) = \rho_{y(t)} e^{j\theta_{y(t)}}$$

where  $\rho_{s(t)}$ ,  $\rho_{x(t)}$ ,  $\rho_{y(t)}$ , and  $\theta_{s(t)}$ ,  $\theta_{x(t)}$ ,  $\theta_{y(t)}$  are the amplitude and phase of the complex signals  $s(t)$ ,  $x(t)$ , and  $y(t)$ , respectively. We let  $M(\rho_{x(t)})$  and  $\Phi(\rho_{x(t)})$  be the normalized AM-AM and AM-PM responses of the HPA due to the input signal  $x(t)$ , then we have

$$y(t) = M(\rho_{x(t)}) e^{j(\theta_{x(t)} + \Phi(\rho_{x(t)}))}$$

Then, the original Saleh's model is extended for HPA by including **eight extra parameters** ( $a_0, a_1, b_0, b_1, \alpha_0, \alpha_1, \beta_0$  and  $\beta_1$ ), resulting in the following generalized equations for  $M(\rho_{x(t)})$  and  $\Phi(\rho_{x(t)})$  as follows.

$$M(\rho_{x(t)}) \equiv \rho_{y(t)} = \frac{\alpha_0 \rho_{x(t)}}{a_0 + \beta_0 (\rho_{x(t)} + b_0)^2}$$

$$\Phi(\rho_{x(t)}) = \frac{\alpha_1 \rho_{x(t)}^2}{a_1 + \beta_1 (\rho_{x(t)} + b_1)^2}$$

We can write  $\exp(j\theta_{x(t)})$  as

$$e^{j\theta_{x(t)}} = \frac{x(t)}{\rho_{x(t)}}$$

$y(t)$  can be further obtained as

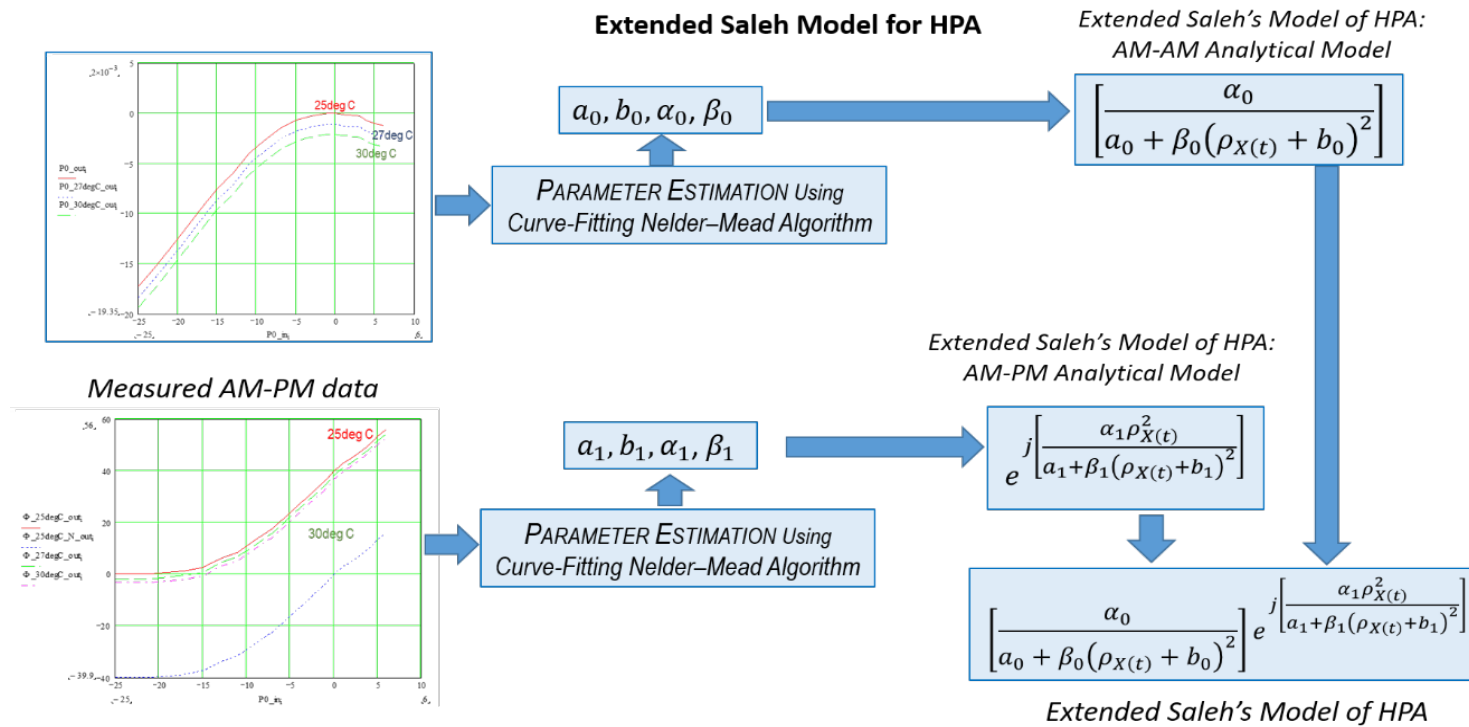
$$y(t) = \left[ \frac{\alpha_0 x(t)}{a_0 + \beta_0 (\rho_{x(t)} + b_0)^2} \right] e^{j \left[ \frac{\alpha_1 \rho_{x(t)}^2}{a_1 + \beta_1 (\rho_{x(t)} + b_1)^2} \right]}$$

It is obvious that the ideal PD output for a given input  $s(t)$  is:

$$= s(t) \left[ \frac{a_0 + \beta_0 (\rho_{x(t)} + b_0)^2}{\alpha_0} \right] e^{-j \left[ \frac{\alpha_1 \rho_{x(t)}^2}{a_1 + \beta_1 (\rho_{x(t)} + b_1)^2} \right]}$$

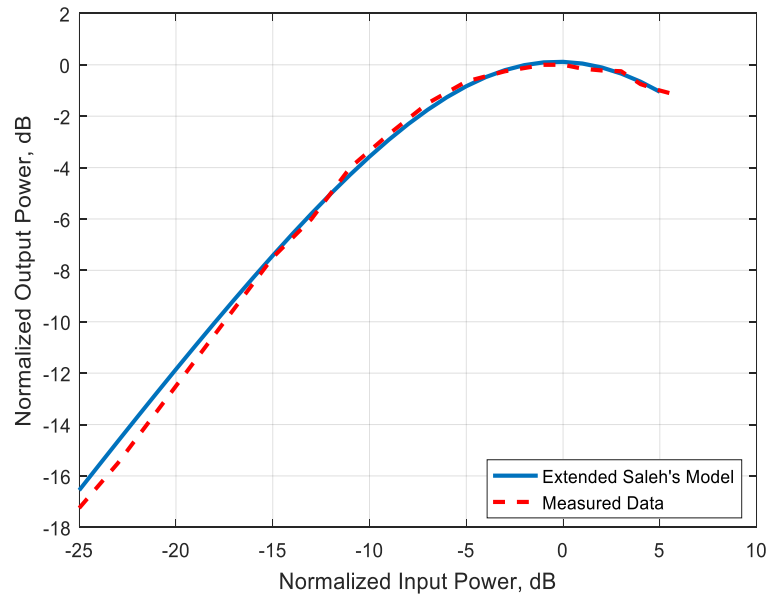
**Extended Saleh's Model was developed in order to accurately characterize a wide range of HPAs, including, L-/S-/X-/Ku-/Ka-band HPAs. The Eight-parameter Model was selected to provide the required accuracy and minimum processing time.**

# Extended Saleh's Model: HPA Modeling

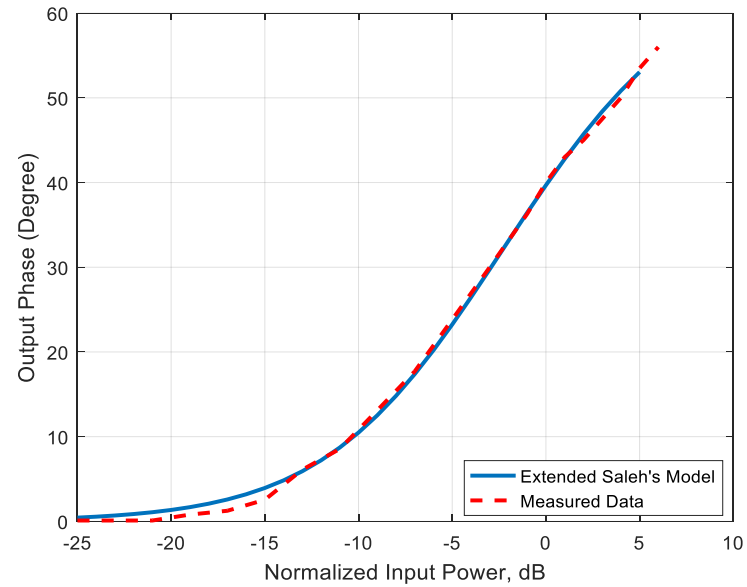


Work flow of achieving unknown parameters using curve-fitting algorithm

# Extended Saleh's Model: HPA Modeling



Normalized output power vs. normalized input power  
for the GBS HPA



Output phase vs. normalized input power  
for the GBS HPA

$$\mathbf{q}_{AM} = \{a_0, b_0, \alpha_0, \beta_0\} = \{3.6407, 0.3063, 11.1163, 4.2947\};$$
$$\mathbf{q}_{PM} = \{a_1, b_1, \alpha_1, \beta_1\} = \{0.4978, 0.1273, 74.6172, 1.0879\}.$$

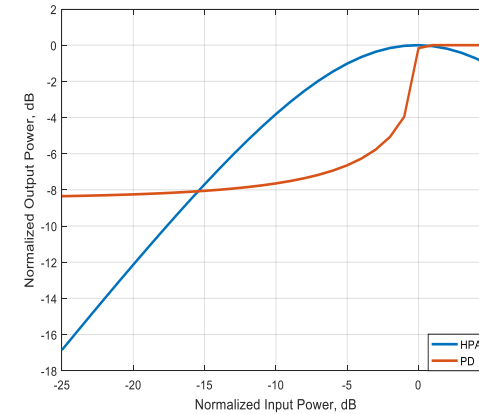
# Extended Saleh's Model: PD Modeling

$$\rho_{PD} = \begin{cases} \frac{(\alpha_0 - 2b_0\beta_0\rho_{x(t)}) - \sqrt{\alpha_0^2 - 4\beta_0\rho_{x(t)}(\alpha_0\rho_{x(t)} + b_0\alpha_0)}}{2\beta_0\rho_{x(t)}^2} & \rho_{x(t)} \leq 1 \\ 1 & \rho_{x(t)} > 1 \end{cases}$$

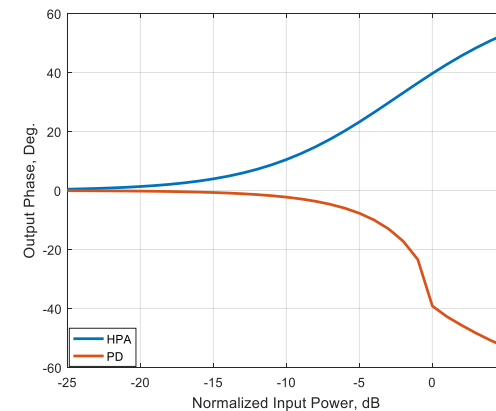
$$\rho_{y(t)} = \rho_{PD} \cdot \rho_{x(t)}$$

$$\theta_{PD} = -\frac{\alpha_1\rho_{y(t)}^2}{a_1 + \beta_1(\rho_{y(t)} + b_1)^2}$$

**Extended Saleh's Model of PD, on which the machine learning based PD designed is developed.**



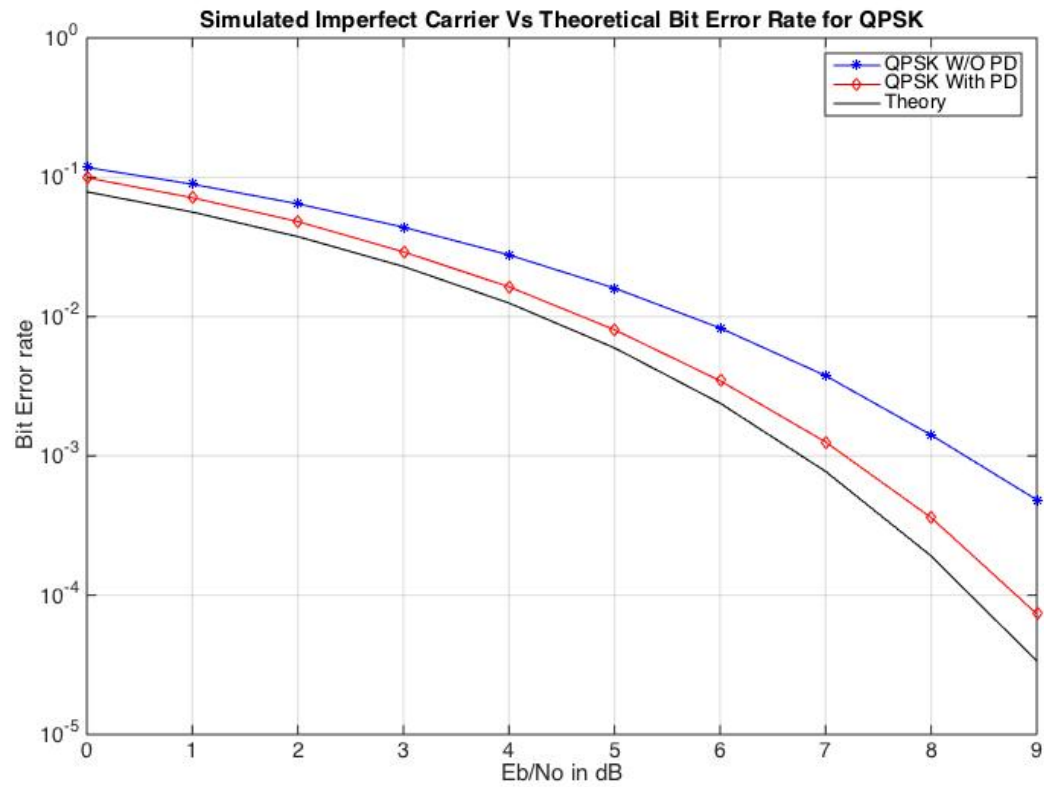
Input and output power relationship of the PD model using extension of Saleh's model for the GBS HPA



Input and output phase relationship of the PD model using extension of Saleh's model for the GBS HPA

# BER Performance Evaluation

- Unfiltered QPSK for assessing the PD's impacts on the waveform at saturation



BER performance for unfiltered QPSK signal passing through a transponder with and without PD at Ka-band

# Outline

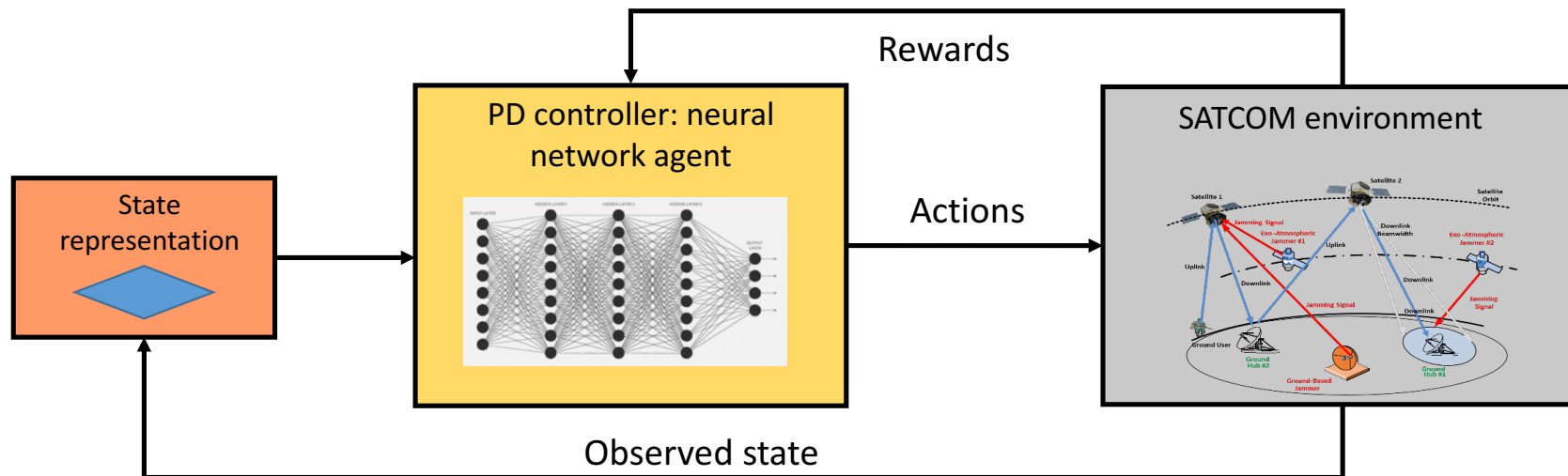
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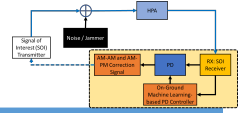
# Machine Learning-based PD Controller

**Reinforcement learning (RL)** is the subfield of machine learning concerned with decision making and optimized control. It studies how an agent can learn and adapt to achieve desired goals in a complex and uncertain environments.

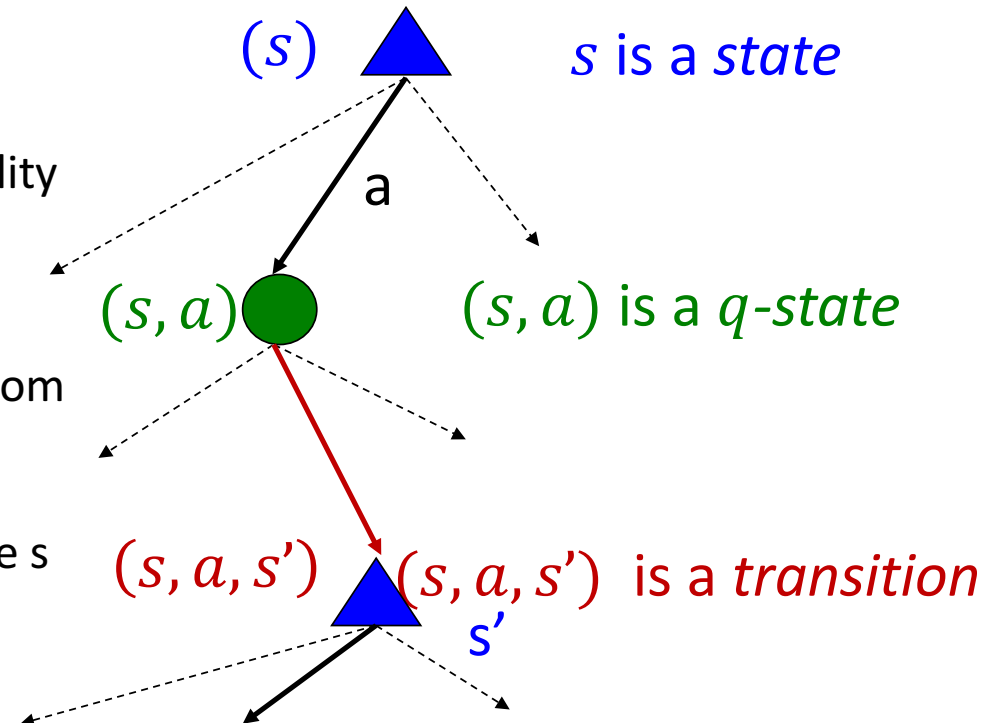


***To develop an effective PD controller, we need to accurately characterize the environment states ( $P_{out}$ ,  $P_{hout}$ ) by differentiating the effects of HPA imperfections and interference signals.***

# Reinforcement Learning Approach

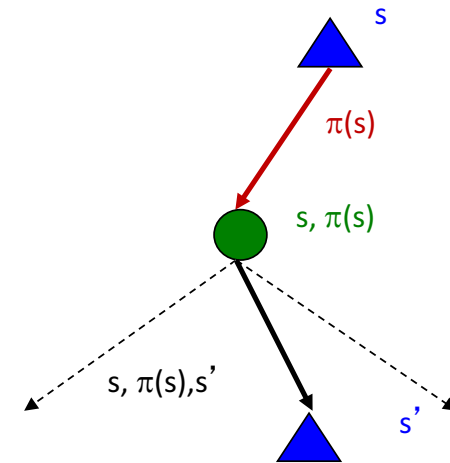
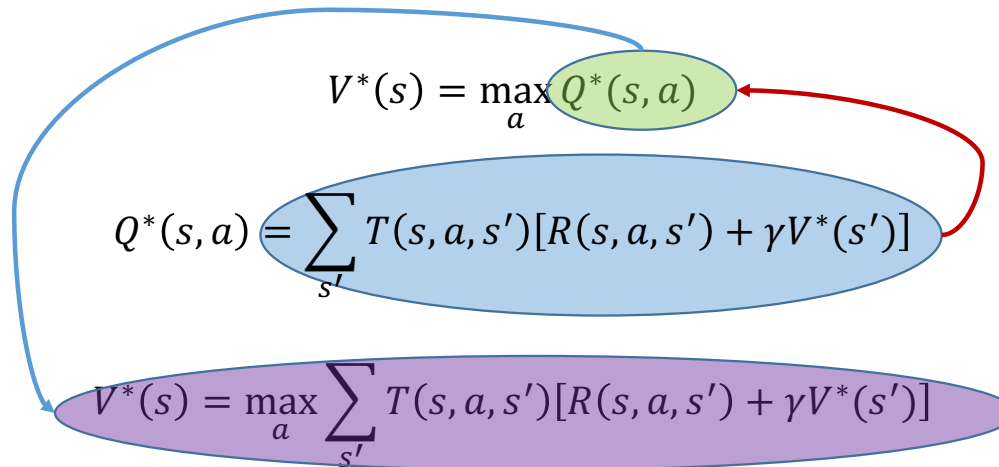


- ❑ The value (utility) of a state  $s - V^*(s)$ : expected utility starting in  $s$  and acting optimally
- ❑ The value (utility) of a q-state  $(s, a) - Q^*(s, a)$ : expected utility starting out having taken action  $a$  from state  $s$  and (thereafter) acting optimally
- ❑ The optimal policy  $-\pi^*(s)$ : optimal action from state  $s$





# Reinforcement Learning Approach



- Simplified Bellman updates calculate  $V$  for a fixed policy,

$$V_0^\pi(s) = 0$$

$$V_{k+1}^\pi(s) \leftarrow \sum_{s'} T(s, \pi(s), s') [R(s, \pi(s), s') + \gamma V^*(s')]$$

- This approach fully exploited the connections between the states
- We need transition  $T$  and reward  $R$

- Q-Learning: sample-based Q-value iteration

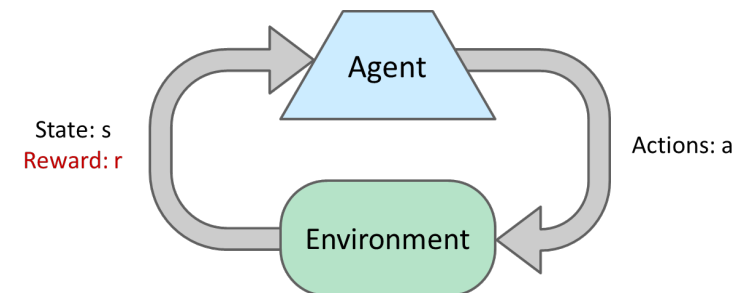
$$Q_{k+1}(s, a) \leftarrow \sum_{s'} T(s, \pi(s), s') [R(s, \pi(s), s') + \gamma \max_{a'} Q_k(s', a')]$$

- Learn  $Q(s, a)$  values as iterations continue,

- Receive a sample  $(s, a, s')$
- Consider your old estimate:  $Q(s, a)$
- Consider your new sample estimate:
 
$$sample = R(s, a, s') + \gamma \max_{a'} Q(s, a')$$
- Incorporate the new estimate into a running average:
 
$$Q(s, a) \leftarrow (1 - \alpha)Q(s, a) + \alpha[sample]$$

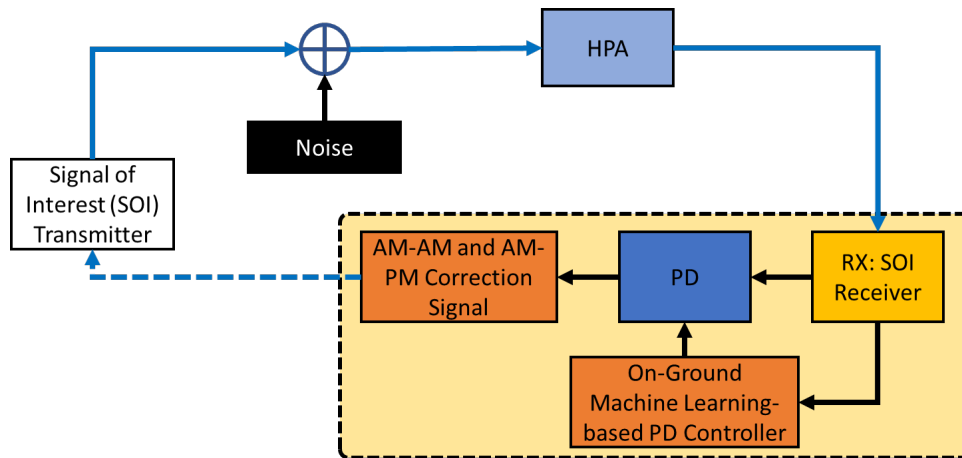
# Reinforcement Learning Approach

- ❑ **Action  $a$ :** the actions the PD takes is to adjust (increase or decrease by certain range) of the 8 parameters of the extended Saleh's model, namely  $(a_0, b_0, \alpha_0, \beta_0)$  and  $(a_1, b_1, \alpha_1, \beta_1)$ .
  - The first four parameters directly correspond to the AM-AM relations, the AM-PM are characterized based on these 8 parameters together.
- ❑ **States  $s$ :** the observable (at least partially) status of the PD Controller's relation with the environment, defined as 2-dimensional continuous states.
  - The feasible set of each parameter is discretized for the algorithm implementation.
- ❑ **Rewards  $r$ :** Given "Input Power" (or  $P_{in}$ ) and "Input Phase" (or  $Phase_{in}$ ), we use the distance between estimated and measured output power and phase of the HPA as the rewards function.
  - $\Delta_p = \sqrt{(P_{out_{obj}} - P_{out_{mea}})^2}$
  - $\Delta_{phase} = \sqrt{(Phase_{out_{obj}} - Phase_{out_{mea}})^2}$
  - Regarding the reward function definition, it can be further simplified by analyzing the characteristics of PD and HPA.



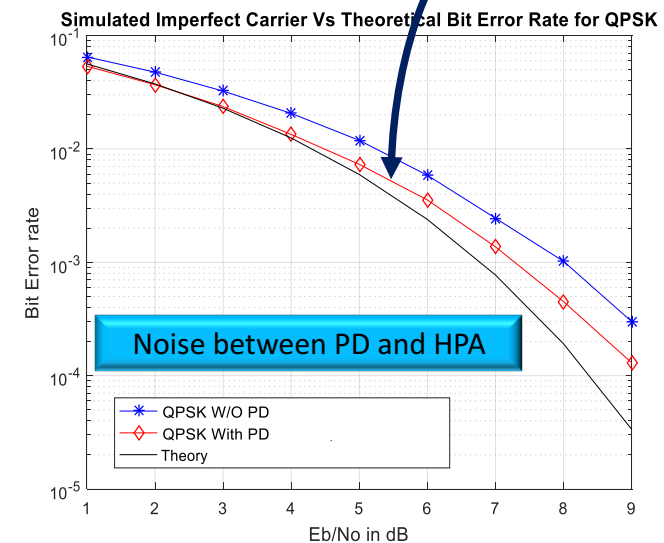
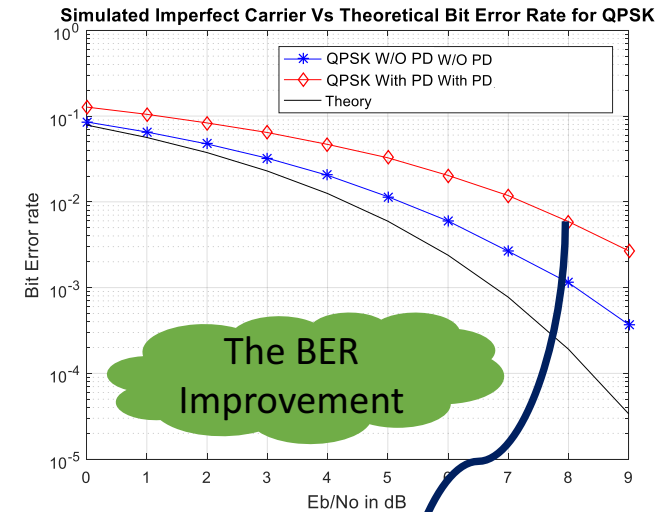
# PD-Scenario 1: Noise Exists between the PD and HPA

- Noise exists between the PD and HPA
- The Noise is characterized based on  $E_b/N_0$
- Machine learning approach is deployed to update the PD parameter set  $(a_0, b_0, \alpha_0, \beta_0, a_1, b_1, \alpha_1, \beta_1)$

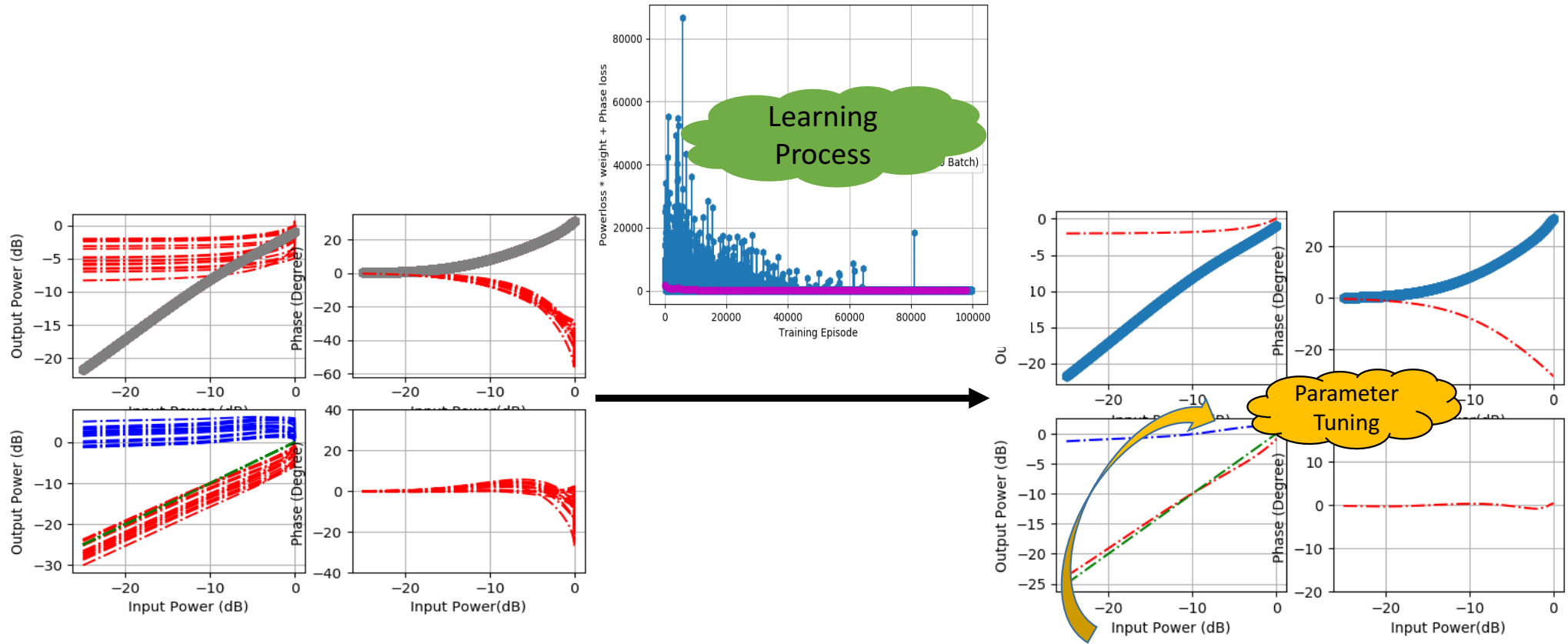


$$a_0 = 10.956 \quad b_0 = 0.1930 \quad \alpha_0 = 15.2576 \quad \beta_0 = 3.4007$$

$$a_1 = 0.2261 \quad b_1 = 0.2354 \quad \alpha_1 = 61.4107 \quad \beta_1 = 1.0755$$



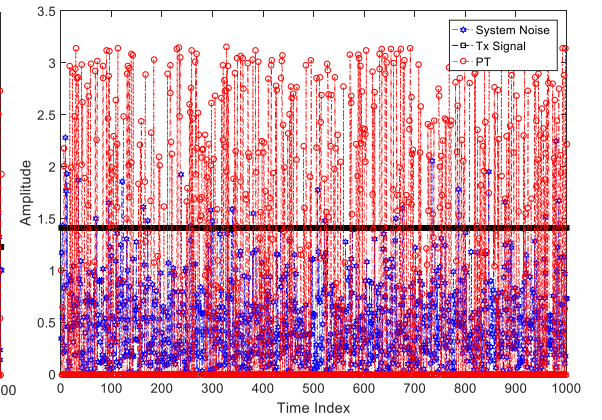
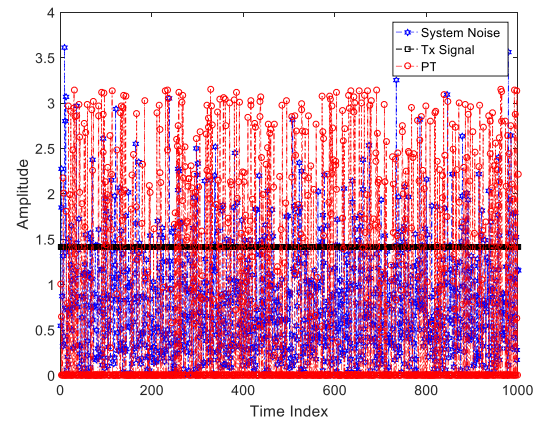
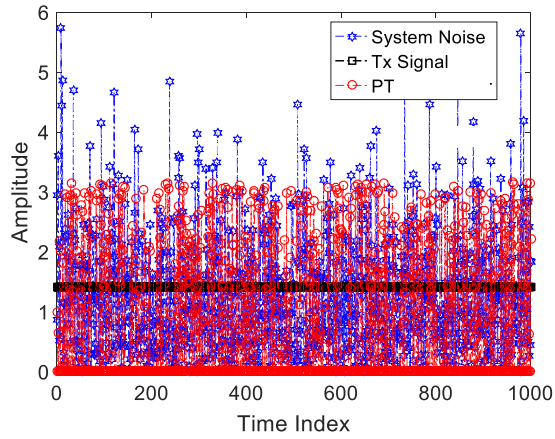
# PD-Scenario 1: PD Parameter Set Learning Process



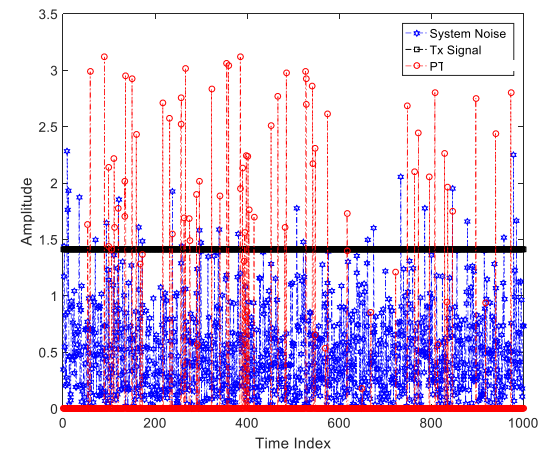
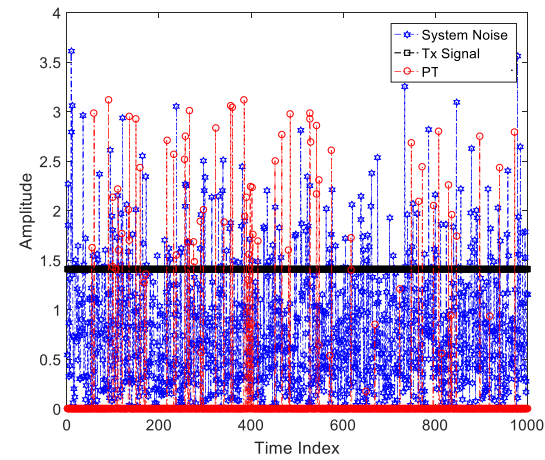
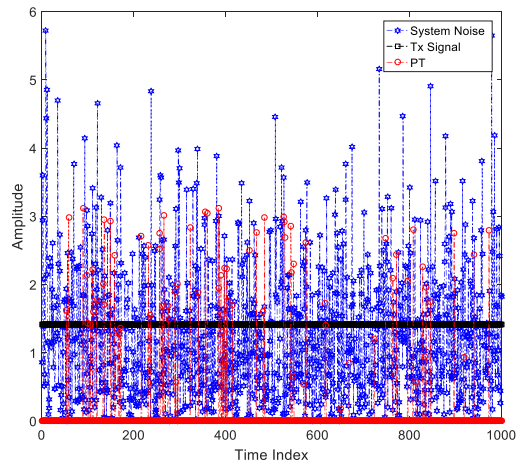
$$\begin{aligned}
 a_0 &= 10.956 & b_0 &= 0.1930 & \alpha_0 &= 15.2576 & \beta_0 &= 3.4007 \\
 a_1 &= 0.2261 & b_1 &= 0.2354 & \alpha_1 &= 61.4107 & \beta_1 &= 1.0755
 \end{aligned}$$

# PD-Scenario 2: Partial Time interference

Active Rate=0.9



Active Rate=0.2



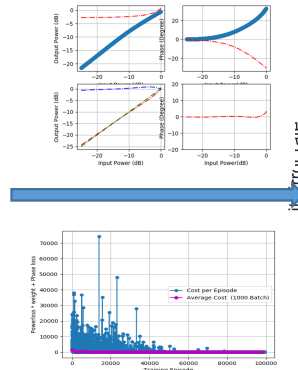
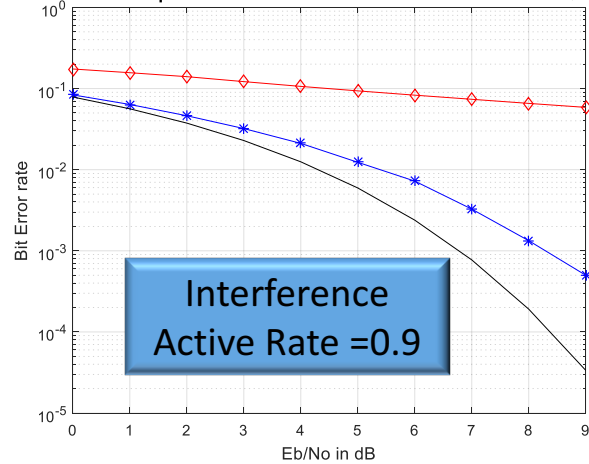
$$\frac{E_b}{N_0} = 1$$

$$\frac{E_b}{N_0} = 5$$

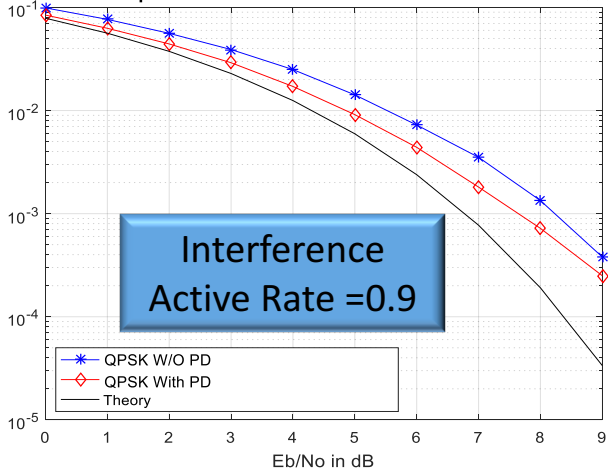
$$\frac{E_b}{N_0} = 9$$

# PD-Scenario 2: Partial Time interference

Simulated Imperfect Carrier Vs Theoretical Bit Error Rate for QPSK

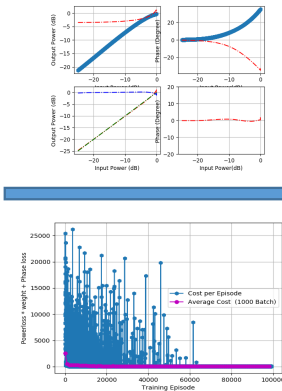
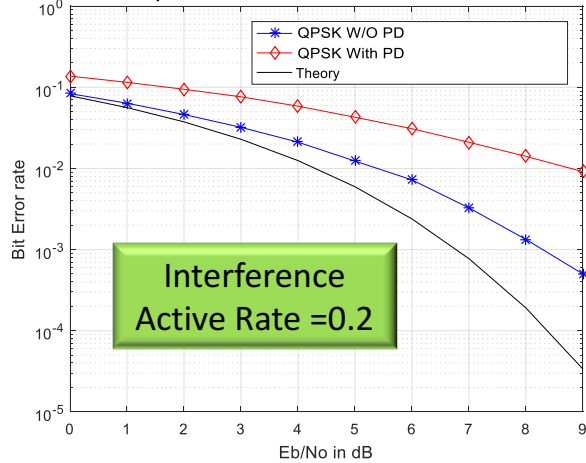


Simulated Imperfect Carrier Vs Theoretical Bit Error Rate for QPSK

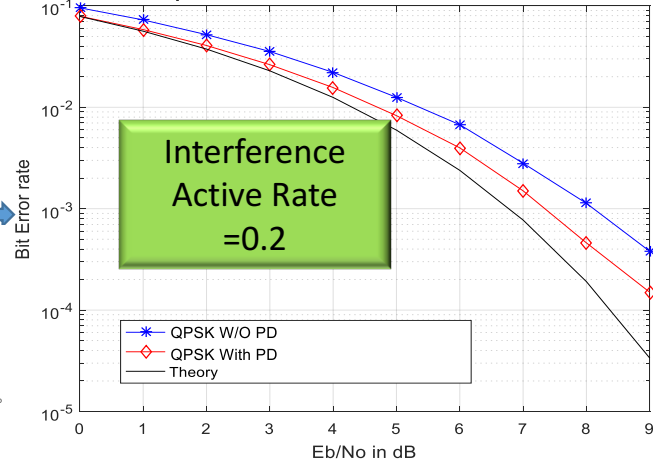


$$\begin{aligned}
 a_0 &= 3.5188 & b_0 &= 0.2621 \\
 \alpha_0 &= 4.9642 & \beta_0 &= 1.0252 \\
 a_1 &= 0.8371 & b_1 &= 0.8371 \\
 \alpha_1 &= 201.77 & \beta_1 &= 4.7948
 \end{aligned}$$

Simulated Imperfect Carrier Vs Theoretical Bit Error Rate for QPSK



Simulated Imperfect Carrier Vs Theoretical Bit Error Rate for QPSK



$$\begin{aligned}
 a_0 &= 12.5052 & b_0 &= 0.3661 \\
 \alpha_0 &= 19.9163 & \beta_0 &= 4.6128 \\
 a_1 &= 0.7536 & b_1 &= 0.0570 \\
 \alpha_1 &= 154.5747 & \beta_1 &= 3.5663
 \end{aligned}$$

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# Conclusions and Future Work

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- *Summaries/Conclusions:*

- Designed a complete SATCOM PD solution with on-ground system modifications to satisfy low-cost demand.
- Mathematically modelled HPA to achieve an excellent agreement with actual AM-AM and AM-PM data, and developed an effective physics-based PD model accordingly.
- Successfully develop a machine-learning based PD controller, which is able to intelligently adjust PD's parameters in the presence of interference signals.
- Assessed BER and spectral regrowth performance of the developed PD by adopting a simplified NPR transponder simulation model.
- The system performance is significantly improved based on our simulation results.

- *Future Work:*

- Develop a database to capture all possible HPA distortions in different operating conditions and associated MODCOD performance.
- Implement the PD design on the hardware.



A word cloud of thank you phrases in various languages. The central and largest text is "thank you" in red. Other prominent words include "danke" (blue), "teşekkür ederim" (pink), "gracias" (green), "merci" (orange), "dank je" (green), "dziękuję" (purple), "obrigado" (green), "sukriya" (purple), "kop khun krap" (green), "arigatō" (pink), "takk" (orange), "dakujem" (orange), "terima kasih" (yellow), "감사합니다" (black), and "ngiyabonga" (red). Numerous smaller words in various colors represent other languages, including "спасибо", "благодарам", "merci", "barka", "welalin", "tack", "paldies", "grazzi", "mahalo", "tapadh iat", "xвала", "asante", "manana", "obrigada", "tenki", "mochchakkeram", "djakuo", "mamnun", "mammun", "sulpay", "go raibh maith agat", "trugarez", "merci", "merce", "merci", "didi", "madloba", "kam sah hamnida", "rahmat", "najis tuke", "tanemirt", "rahmet", "xiexie", "ευχαριστώ", "diolch", "dhanyavadagalau", "shukriya", "merce", "merci", "mami", "nandri", "kiitos", "dankie", "mauruuru", "koszonom", "hvala", "sagolun", "chnorakaloutioun", "gratias ago", "gracies", "sulpay", "taiku", "griez", "arigatō", "takk", "dakujem", "trugarez", "merci", "merce", "merci", "didi", "madloba", "kam sah hamnida", "rahmat", "najis tuke", "tanemirt", "rahmet", "xiexie", "ευχαριστώ", "diolch", "dhanyavadagalau", "shukriya", "merce", "merci".